

## Module 7 Quadrilaterals

Monday, April 7, 2025 11:56 PM

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Quadrilater...

# Module 7: Quadrilaterals Geometry

### Content Objective

Students apply and prove theorems about the properties of parallelograms.

Students use the properties of rectangles to determine whether a parallelogram is a rectangle and to write proofs.

Students apply and prove the properties of rhombi and squares.

Students recognize and apply the properties of trapezoids and

kites.

#### **MA.912.GR.1.4**

Prove relationships and theorems about parallelograms. Solve mathematical and real-world problems involving postulates, relationships and theorems of parallelograms.

#### **MA.912.GR.3.2**

Given a mathematical context, use coordinate geometry to classify or justify definitions, properties and theorems involving circles, triangles or quadrilaterals.

#### **MA.912.GR.3.3**

Use coordinate geometry to solve mathematical and real-world geometric problems involving lines, circles, triangles and quadrilaterals.

#### **MA.912.GR.1.5**

Prove relationships and theorems about trapezoids. Solve mathematical and real-world problems involving postulates, relationships and theorems of trapezoids.

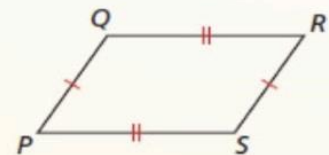
### Theorems

#### **Theorem 7.3 Parallelogram Opposite Sides Theorem**

If a quadrilateral is a parallelogram, then its opposite sides are congruent.

If  $PQRS$  is a parallelogram, then  $\overline{PQ} \cong \overline{RS}$  and  $\overline{QR} \cong \overline{SP}$ .

*Proof* p. 368

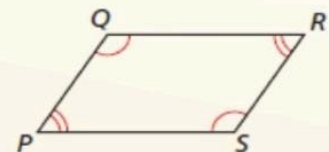


#### **Theorem 7.4 Parallelogram Opposite Angles Theorem**

If a quadrilateral is a parallelogram, then its opposite angles are congruent.

If  $PQRS$  is a parallelogram, then  $\angle P \cong \angle R$  and  $\angle Q \cong \angle S$ .

*Proof* Ex. 37, p. 373



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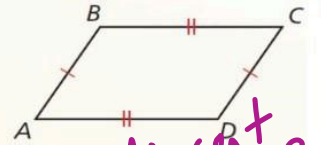
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## Theorems

### Theorem 7.7 ~~Parallelogram~~ Opposite Sides Converse

If both pairs of opposite sides of a quadrilateral are congruent, then the quadrilateral is a parallelogram.

If  $\overline{AB} \cong \overline{CD}$  and  $\overline{BC} \cong \overline{DA}$ , then  $ABCD$  is a parallelogram.

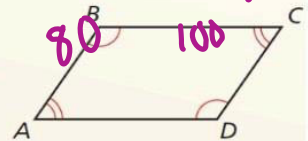


### Theorem 7.8 ~~Parallelogram~~ Opposite Angles Converse

If both pairs of opposite angles of a quadrilateral are congruent, then the quadrilateral is a parallelogram.

If  $\angle A \cong \angle C$  and  $\angle B \cong \angle D$ , then  $ABCD$  is a parallelogram.

*Proof* Ex. 39, p. 383



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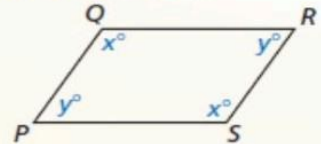
## Theorems

### Theorem 7.5 ~~Parallelogram~~ Consecutive Angles Theorem

If a quadrilateral is a parallelogram, then its consecutive angles are supplementary.

If  $PQRS$  is a parallelogram, then  $x^\circ + y^\circ = 180^\circ$ .

*Proof* Ex. 38, p. 373

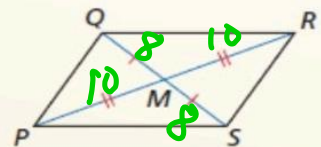


### Theorem 7.6 ~~Parallelogram~~ Diagonals Theorem

If a quadrilateral is a parallelogram, then its diagonals bisect each other.

If  $PQRS$  is a parallelogram, then  $\overline{QM} \cong \overline{SM}$  and  $\overline{PM} \cong \overline{RM}$ .

*Proof* p. 370



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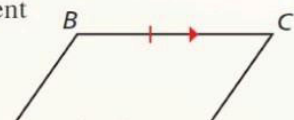
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## Theorems

### Theorem 7.9 ~~Opposite Sides~~ Parallel and Congruent Theorem

If one pair of opposite sides of a quadrilateral are congruent and parallel, then the quadrilateral is a parallelogram.

If  $\overline{BC} \parallel \overline{AD}$  and  $\overline{BC} \cong \overline{AD}$ , then  $ABCD$  is a parallelogram.





a parallelogram.

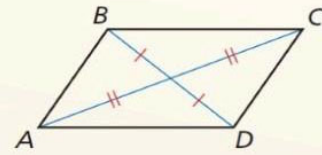
*Proof* Ex. 40, p. 383

### Theorem 7.10 Parallelogram Diagonals Converse

If the diagonals of a quadrilateral bisect each other, then the quadrilateral is a parallelogram.

If  $\overline{BD}$  and  $\overline{AC}$  bisect each other, then  $ABCD$  is a parallelogram.

*Proof* Ex. 41, p. 383

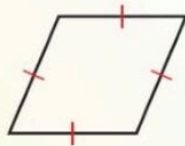


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## Core Concept

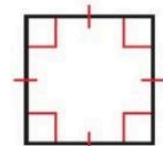
### Rhombuses, Rectangles, and Squares



A **rhombus** is a parallelogram with four congruent sides.



A **rectangle** is a parallelogram with four right angles.



A **square** is a parallelogram with four congruent sides and four right angles.



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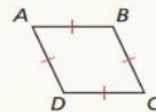
## Corollaries

### Corollary 7.2 Rhombus Corollary

A quadrilateral is a rhombus if and only if it has four congruent sides.

$ABCD$  is a rhombus if and only if  $\overline{AB} \cong \overline{BC} \cong \overline{CD} \cong \overline{AD}$ .

*Proof* Ex. 81, p. 396

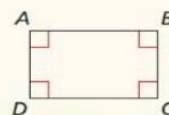


### Corollary 7.3 Rectangle Corollary

A quadrilateral is a rectangle if and only if it has four right angles.

$ABCD$  is a rectangle if and only if  $\angle A$ ,  $\angle B$ ,  $\angle C$ , and  $\angle D$  are right angles.

*Proof* Ex. 82, p. 396



### Corollary 7.4 Square Corollary

A quadrilateral is a square if and only if it is a rhombus and a rectangle.

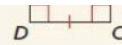
$ABCD$  is a square if and only if





$\overline{AB} \cong \overline{BC} \cong \overline{CD} \cong \overline{AD}$  and  $\angle A$ ,  $\angle B$ ,  $\angle C$ ,  
and  $\angle D$  are right angles.

*Proof* Ex. 83, p. 396



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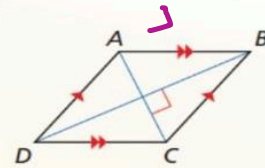
## Theorems

### ~~Theorem 7.11 Rhombus Diagonals Theorem~~

A parallelogram is a rhombus if and only if its diagonals are perpendicular.

$\square ABCD$  is a rhombus if and only if  $\overline{AC} \perp \overline{BD}$ .

*Proof* p. 390; Ex. 72, p. 395

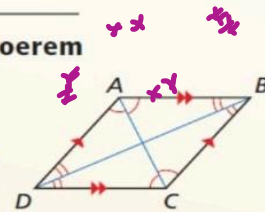


### ~~Theorem 7.12 Rhombus Opposite Angles Theorem~~

A parallelogram is a rhombus if and only if each diagonal bisects a pair of opposite angles.

$\square ABCD$  is a rhombus if and only if  $\overline{AC}$  bisects  $\angle BCD$  and  $\angle BAD$ , and  $\overline{BD}$  bisects  $\angle ABC$  and  $\angle ADC$ .

*Proof* Exs. 73 and 74, p. 395



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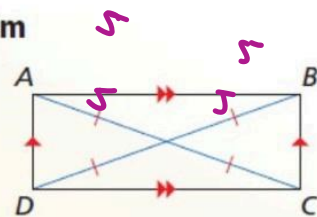
## Theorem

### Theorem 7.13 Rectangle Diagonals Theorem

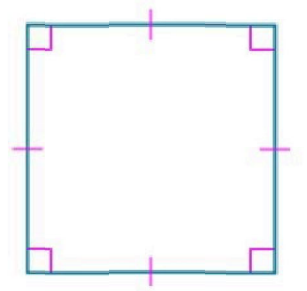
A parallelogram is a rectangle if and only if its diagonals are congruent.

$\square ABCD$  is a rectangle if and only if  $\overline{AC} \cong \overline{BD}$ .

*Proof* Exs. 87 and 88, p. 396



A **square** is a parallelogram with all four sides and all four angles congruent. All of the properties of parallelograms, rectangles, and rhombi apply to squares. For example, the diagonals of a square bisect each other (parallelogram), are congruent (rectangle), and are perpendicular (rhombus).



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### Theorems: Conditions for Rhombi and Squares

#### Theorem 7.17

If the diagonals of a parallelogram are perpendicular, then the parallelogram is a **square, rectangle, rhombus**

#### Theorem 7.18

If one diagonal of a parallelogram bisects a pair of opposite angles, then the parallelogram is a **rhombus, square**

#### Theorem 7.19

If two consecutive sides of a parallelogram are congruent, then the parallelogram is a **square, rhombus**

#### Theorem 7.20

If a quadrilateral is both a rectangle and a rhombus, then it is a **square**

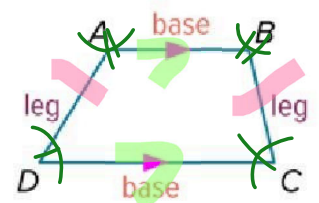


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A **trapezoid** is a quadrilateral with **at least one pair of parallel sides**. In a trapezoid that is not a parallelogram, the parallel sides are called the **bases** and the nonparallel sides are called **legs**.

A **base angle** is formed by a base and a leg. In





trapezoid  $ABCD$ ,  $\angle A$  and  $\angle B$  are one pair of base angles, and  $\angle C$  and  $\angle D$  are the other pair. If the legs are congruent, then a trapezoid is an **isosceles trapezoid**.

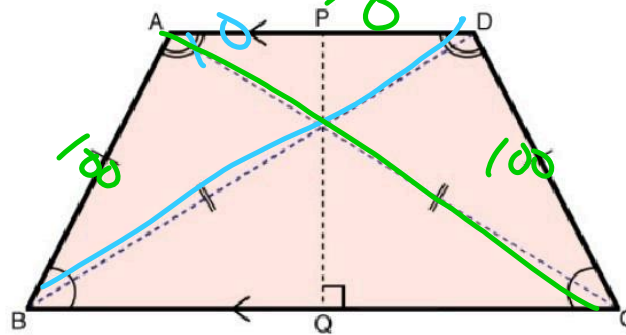


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## Properties of an Isosceles Trapezoid

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- ① Has one pair of parallel and unequal opposite sides (bases)
- ② Has one pair of congruent non-parallel sides (legs)
- ③ Lower base angles & upper base angles are congruent
- ④ Diagonals are congruent
- ⑤ Any lower base angle is supplementary to any upper base angle
- ⑥ Has one line of symmetry connecting the bases at their midpoints



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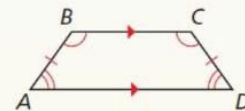
## Theorems

### Theorem 7.14 Isosceles Trapezoid Base Angles Theorem

If a trapezoid is isosceles, then each pair of base angles is congruent.

If trapezoid  $ABCD$  is isosceles, then  $\angle A \cong \angle D$  and  $\angle B \cong \angle C$ .

*Proof* Ex. 39, p. 405



### Theorem 7.15 Isosceles Trapezoid Base Angles Converse

If a trapezoid has a pair of congruent base angles, then it is an isosceles trapezoid.

If  $\angle A \cong \angle D$  (or if  $\angle B \cong \angle C$ ), then trapezoid  $ABCD$  is isosceles.

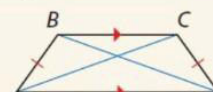
*Proof* Ex. 40, p. 405



### Theorem 7.16 Isosceles Trapezoid Diagonals Theorem

A trapezoid is isosceles if and only if its diagonals are congruent.

Trapezoid  $ABCD$  is isosceles if and only if  $\overline{AC} \cong \overline{BD}$ .





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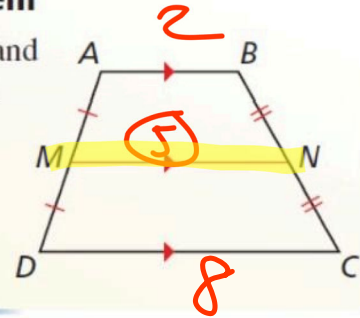
## Theorem

### Theorem 7.17 Trapezoid Midsegment Theorem

The midsegment of a trapezoid is parallel to each base, and its length is one-half the sum of the lengths of the bases.

If  $\overline{MN}$  is the midsegment of trapezoid  $ABCD$ , then  $\overline{MN} \parallel \overline{AB}$ ,  $\overline{MN} \parallel \overline{DC}$ , and  $MN = \frac{1}{2}(AB + CD)$ .

Proof Ex. 49, p. 406



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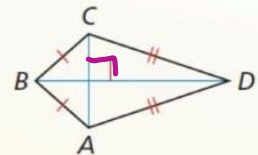
## Theorems

### Theorem 7.18 Kite Diagonals Theorem

If a quadrilateral is a kite, then its diagonals are perpendicular.

If quadrilateral  $ABCD$  is a kite, then  $\overline{AC} \perp \overline{BD}$ .

Proof p. 401

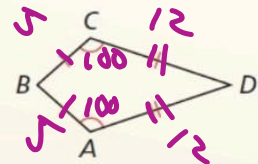


### Theorem 7.19 Kite Opposite Angles Theorem

If a quadrilateral is a kite, then exactly one pair of opposite angles are congruent.

If quadrilateral  $ABCD$  is a kite and  $\overline{BC} \cong \overline{BA}$ , then  $\angle A \cong \angle C$  and  $\angle B \not\cong \angle D$ .

Proof Ex. 47, p. 406



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Kites

A **kite** is a convex quadrilateral with exactly two distinct pairs of



adjacent congruent sides. Unlike a parallelogram, the opposite sides of a kite are not congruent or parallel.

### Theorems: Kites

#### Theorem 7.25

If a quadrilateral is a kite, then its diagonals are perpendicular.

#### Theorem 7.26

If a quadrilateral is a kite, then exactly one pair of opposite angles is congruent.



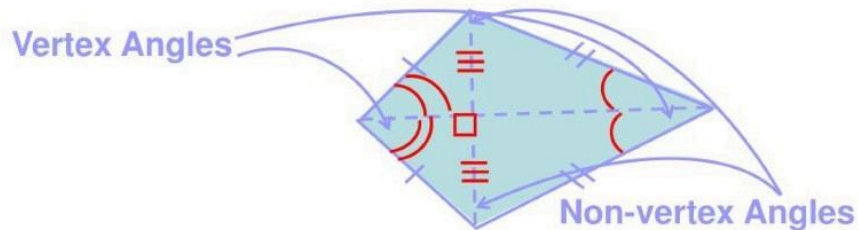
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## Properties of Kites and Trapezoids

Kite:

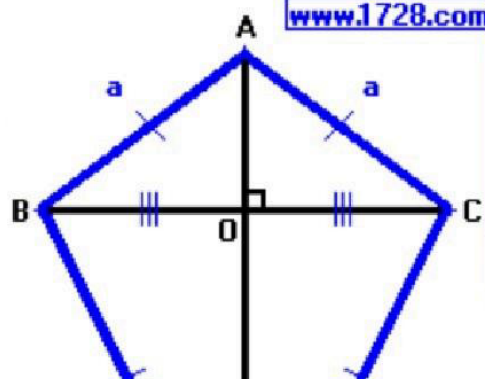
- *2 distinct pairs of consecutive congruent sides.*
- One diagonal is the  $\perp$  bisector of the other.
- Non-vertex angles are congruent.
- One diagonal bisects both vertex angles.



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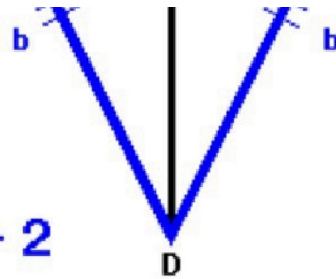
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$\angle A$  and  $\angle D$  are vertex angles.  
 $\angle B$  and  $\angle C$  are the non-vertex angles.  
Lines AD and BC are diagonals and always meet at right angles  
Line AD, the axis of symmetry, bisects diagonal BC, bisects  $\angle A$  and  $\angle D$  and bisects the kite into 2 congruent triangles:  
 $\triangle ABD$  and  $\triangle ACD$



Side AB = side AC  
Side BD = side CD  
Line OB = Line OC  
Diagonal BC bisects the kite  
into 2 isosceles triangles

$$\text{Kite Area} = (AD \times BC) \div 2$$

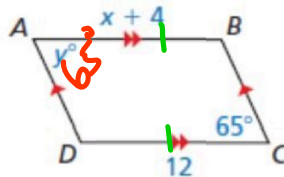


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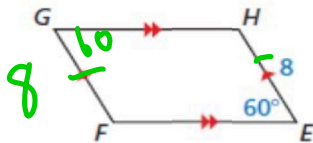
\*Find all angles and side measures for all problems on this page!

Find the values of  $x$  and  $y$ .

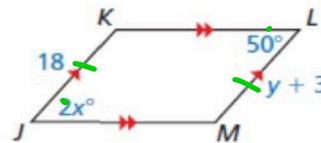


$$\begin{aligned} x+4 &= 12 \\ -4 &-4 \\ \hline x &= 8 \end{aligned}$$

1. Find  $FG$  and  $m \angle G$ .



2. Find the values of  $x$  and  $y$ .



$$\begin{aligned} y+3 &= 18 \\ -3 &-3 \\ \hline y &= 15 \end{aligned}$$

$$\begin{aligned} 2x &= 50 \\ \frac{2x}{2} &= \frac{50}{2} \\ x &= 25 \end{aligned}$$



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## Example 2

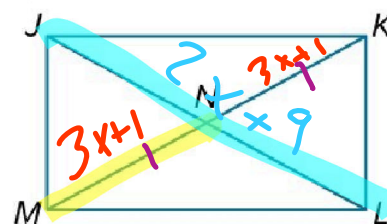
Use Properties of Rectangles and Algebra

Check

Quadrilateral JKLM is a rectangle.

Part A

If  $MN = 3x + 1$  and  $JL = 2x + 9$ , find  $MK$ . Round to the nearest tenth if necessary.



$$x = 1.8$$

$$\begin{aligned} 6x+2 &= 2x+9 \\ -2x &-2x \\ \hline 4x+2 &= 9 \end{aligned}$$





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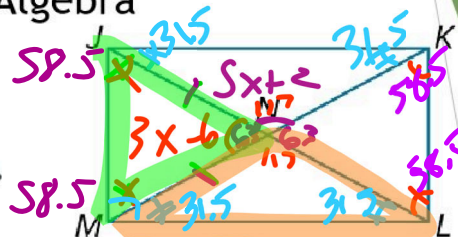
$$\frac{4x}{4} = \frac{7}{4}$$

## Example 2

Use Properties of Rectangles and Algebra

Check

Quadrilateral JKLM is a rectangle.



Part B

If  $m\angle JNK = (5x + 2)^\circ$  and  $m\angle JNM = (3x - 6)^\circ$ ,

find  $m\angle JNK$  and  $m\angle JNM$ . Part C: Find all angle degrees!

$$x = 23$$

$$3x - 6 + 5x + 2 = 180$$

$$8x - 4 = 180$$

$$8x = 184$$

$$\frac{8x}{8} = \frac{184}{8}$$



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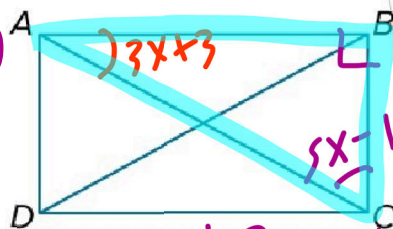
## Example 2

$$180 - 90 = 90$$

Quadrilateral ABCD is a rectangle.

If  $m\angle BAC = (3x + 3)^\circ$  and

$m\angle ACB = (5x - 1)^\circ$ , find the value of  $x$ .



$$3x + 3 + 5x - 1 = 90$$

$$\frac{8x + 2}{2} = \frac{90}{2}$$

$$\frac{8x}{8} = \frac{88}{8} \quad x = 11$$



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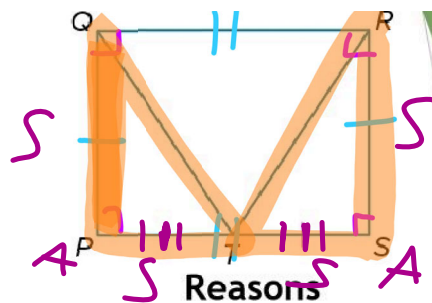
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### Example 3

Prove Rectangular Relationships

Given:  $PQRS$  is a rectangle;  $\overline{PT} \cong \overline{ST}$ .

Prove:  $\overline{QT} \cong \overline{RT}$



#### Statements

1.  $PQRS$  is a rectangle;  $\overline{PT} \cong \overline{ST}$

2.  $PQRS$  is a parallelogram

3.  $\overline{QP} \cong \overline{RS}$  and  $\overline{PS} \cong \overline{QR}$

4.  $\angle Q, \angle R, \angle P, \angle S = 90^\circ$  Right  $\angle$ s

5.  $\angle S \cong \angle P$

6.  $\triangle QPT \cong \triangle RST$

7.  $\overline{QT} \cong \overline{RT}$

1. Given

2. Definition of rectangle

3. Opp. sides of a  $\square$  are  $\cong$ .

4. Definition of rectangle

5. All right angles are congruent.

6. SAS

7. CPCTC

corresponding parts of

congruent triangles are congruent

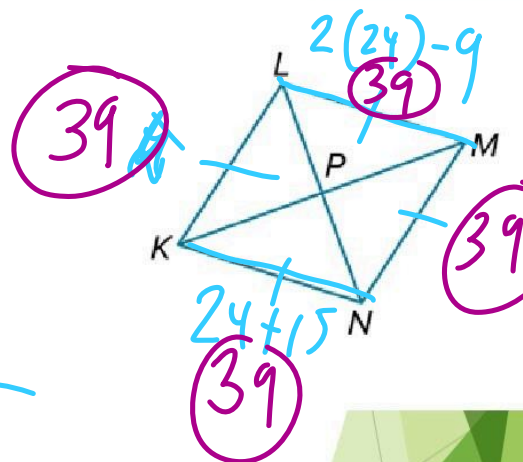
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If  $LM = 2x - 9$  and  $KN = x + 15$  in rhombus  $KLMN$ , find the value of  $x$ .

Find all side lengths!

$$\begin{array}{r} 2x - 9 = x + 15 \\ -x \quad \quad -x \\ \hline x - 9 = 15 \\ +9 \quad +9 \\ \hline x = 24 \end{array}$$



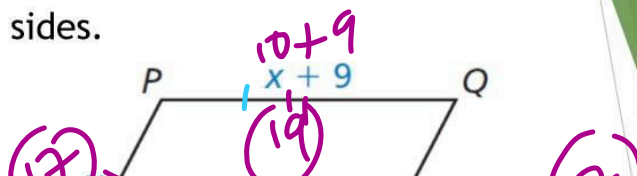
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For what values of  $x$  and  $y$  is quadrilateral  $PQRS$  a parallelogram?

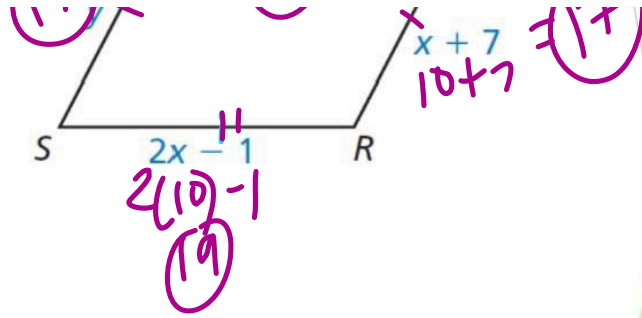
Find the lengths of all the sides.

$$\begin{array}{r} x + 9 = 2x - 1 \\ -x \quad \quad -x \\ \hline 9 = x - 1 \end{array}$$





$$\begin{array}{r} 9 = x - 1 \\ +1 \quad +1 \\ \hline 10 = x \end{array}$$

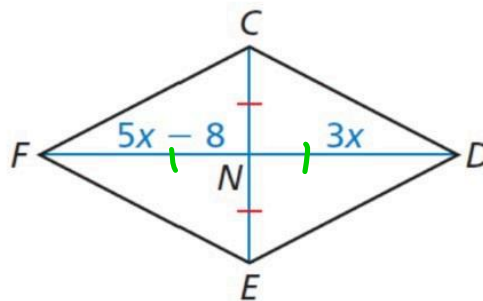


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For what value of  $x$  is quadrilateral  $CDEF$  a parallelogram?

$$\begin{array}{r} 5x - 8 = 3x \\ -5x \quad -5x \\ \hline -8 = -2x \\ \div 2 \quad \div 2 \\ \hline 4 = x \end{array}$$



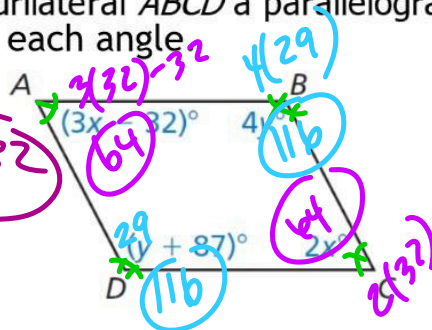
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For what values of  $x$  and  $y$  is quadrilateral  $ABCD$  a parallelogram?  
Determine the measures of each angle

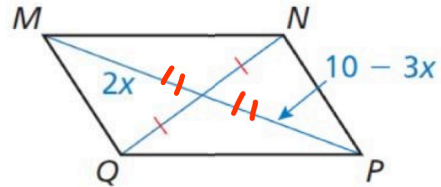
$$\begin{array}{r} 3x - 32 = -2x \\ -3x \quad -3x \\ \hline -32 = -1x \\ \hline x = 32 \end{array}$$

$$\begin{array}{r} -y + 87 = 4y \\ -y \quad -y \\ \hline 87 = 5y \\ \div 5 \quad \div 5 \\ \hline 17.4 = y \end{array}$$



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For what value of  $x$  is quadrilateral  $MNPQ$  a parallelogram?

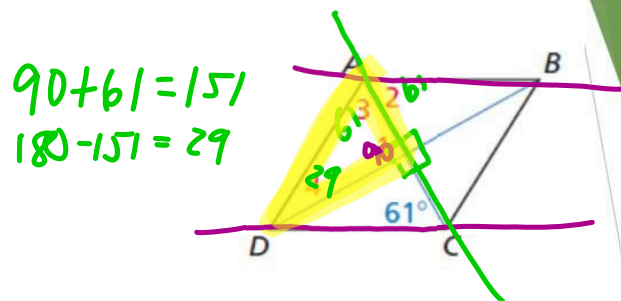


$$\begin{array}{r} 2x = 10 - 3x \\ + 3x \quad \quad + 3x \\ \hline 5x = 10 \\ x = 2 \end{array}$$

$$\begin{array}{r} 10 - 3x = 2x \\ + 3x \quad + 3x \\ \hline 10 = 5x \\ \frac{10}{5} = \frac{5x}{5} \end{array} \quad x = 2$$

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Find the measures of the numbered angles in rhombus  $ABCD$ .





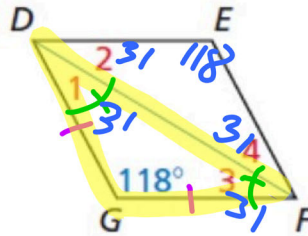


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Find the measures of the numbered angles in rhombus  $DEFG$ .

$$\begin{array}{r} 180 \\ -118 \\ \hline 62 \\ \div 2 = 31 \end{array}$$



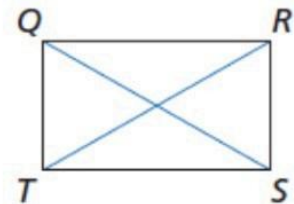
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In rectangle  $QRST$ ,  $QS = 5x - 31$  and  $RT = 2x + 11$ .  
Find the lengths of the diagonals of  $QRST$ .

39

$$\begin{array}{r} 5x - 31 = 2x + 11 \\ -2x \quad -2x \\ \hline 3x - 31 = 11 \\ +31 \quad +31 \\ \hline 3x = 42 \\ \div 3 \quad \div 3 \\ \hline x = 14 \end{array}$$



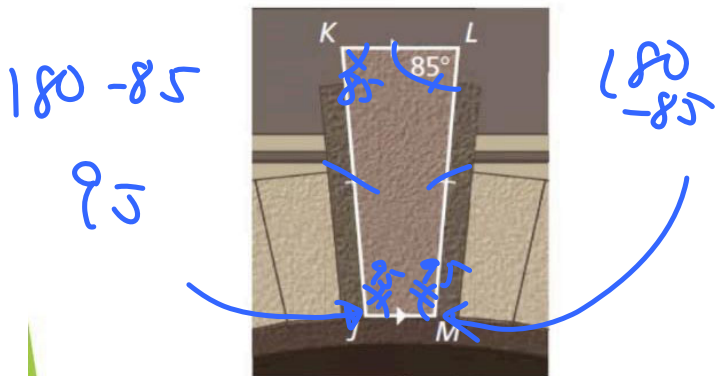
$x = 14$



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The stone above the arch in the diagram is an isosceles trapezoid. Find  $m\angle K$ ,  $m\angle M$ , and  $m\angle J$ .



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**MUSIC** The body of the guitar shown is a trapezoidal prism. The front face of the guitar is an isosceles trapezoid.

$AB = 3x - 2$ ,  $CD = 3x + 9$ ,

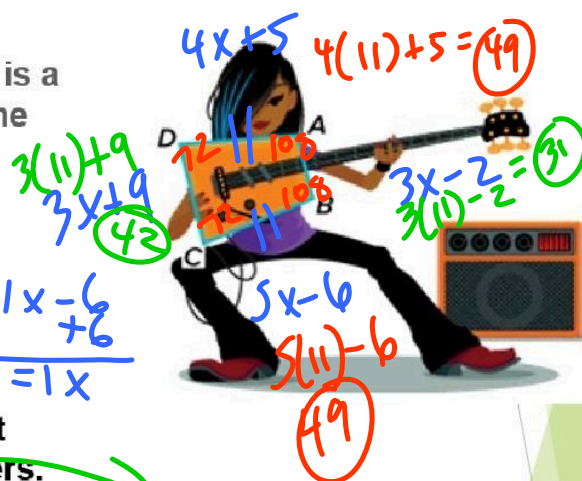
$AD = 4x + 5$ , and  $BC = 5x - 6$ .

Part A Prove  $x = 11$ .

Part B Find  $m\angle A$  if  $m\angle C = 72^\circ$ .

Part C Find the perimeter of the front face of the guitar in centimeters.

Handwritten green calculation:  $49 + 49 + 31 + 42 = 171 \text{ cm}$

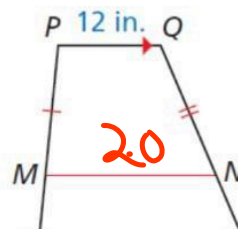


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In the diagram,  $\overline{MN}$  is the midsegment of trapezoid  $PQRS$ . Find  $MN$ .

Handwritten red calculation:  $28 + 12 = \frac{40}{2} = 20$



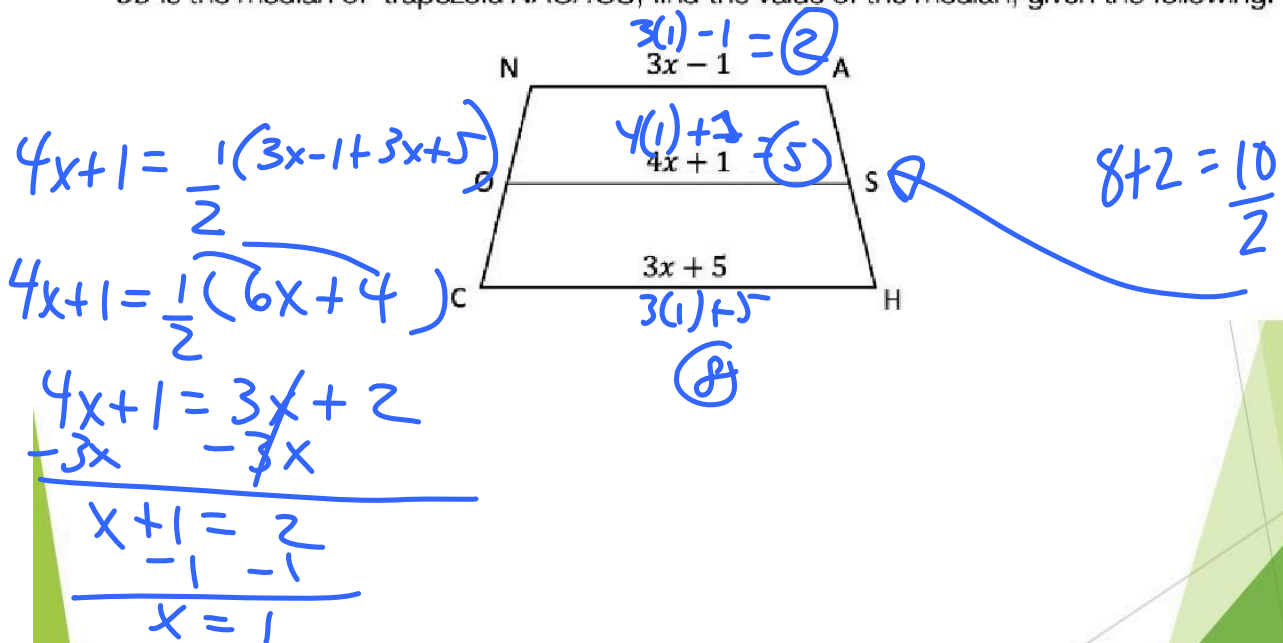




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$\overline{DS}$  is the median of trapezoid NACHOS, find the value of the median, given the following:



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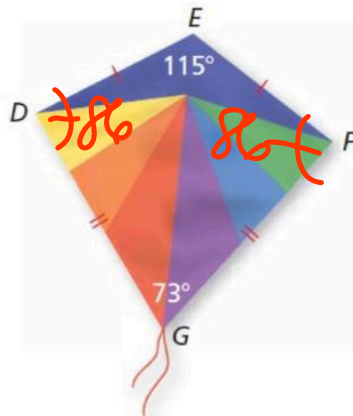
Find  $m\angle D$  in the kite shown.

Find  $m\angle F$  in the kite.

$$115 + 73 = 188$$

$$360 - 188 = 172$$

$$172 \div 2 = 86$$



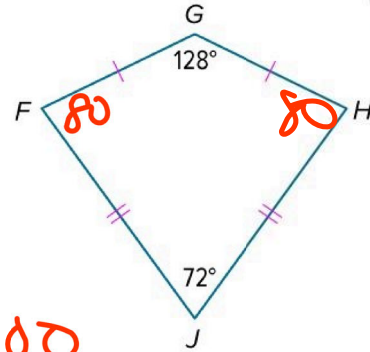


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### Example 6

Find Angle Measures in Kites



Check

If  $FGHJ$  is a kite, find  $m\angle F$ .

Also find  $m\angle H$

$$\begin{aligned}
 &72 + 128 = 200 \\
 &\frac{360}{-} \frac{200}{160} \div 2 = 80
 \end{aligned}$$



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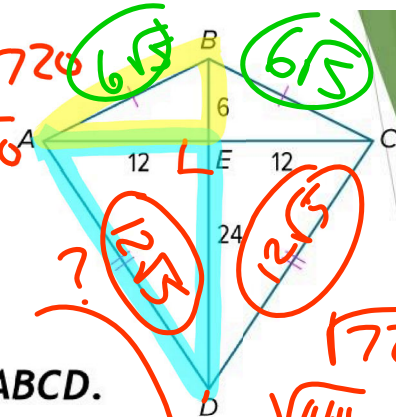
### Example 7

Find Lengths in Kites

Quadrilateral  $ABCD$  is a kite.

Part A Find  $AD$ .

Part B Find the perimeter of kite  $ABCD$ .



$$\begin{aligned}
 c^2 &= a^2 + b^2 \\
 c^2 &= 6^2 + 12^2 \\
 c^2 &= 36 + 144 \\
 c^2 &= 180
 \end{aligned}$$

$$\begin{aligned}
 &\sqrt{180} \\
 &= \sqrt{36 \cdot 5} \\
 &= 6\sqrt{5}
 \end{aligned}$$

$$\begin{aligned}
 &12 + 12 + 6 + 6 \\
 &= 36
 \end{aligned}$$



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In a kite, the measures of the angles are  $3x^\circ$ ,  $75^\circ$ ,  $90^\circ$ , and  $120^\circ$ . Find the value of  $x$ . What are the measures of the angles that are congruent?

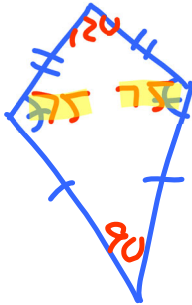
$$3x + 75 + 90 + 120 = 360$$

$$3x + 285 = 360$$

$$\begin{array}{r} -285 \\ \hline 3x = 75 \end{array}$$

$$\frac{3x}{3} = \frac{75}{3}$$

$$x = 25$$



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Kite's Perimeter = 86 ft.

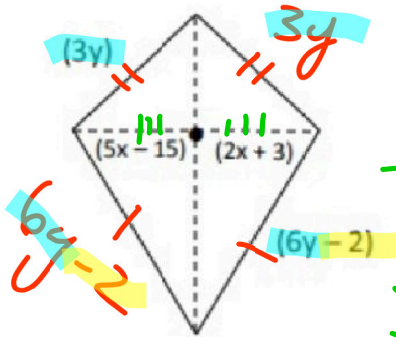
Determine the value of  $x$  and  $y$ .

$$18y - 4 = 86$$

$$\begin{array}{r} +4 \\ \hline 18y = 90 \end{array}$$

$$\frac{18y}{18} = \frac{90}{18}$$

$$y = 5$$



$$5x - 15 = 2x + 3$$

$$\begin{array}{r} +15 \\ \hline 5x = 2x + 18 \end{array}$$

$$\begin{array}{r} 5x = 2x + 18 \\ -2x \\ \hline 3x = 18 \end{array}$$

$$\frac{3x}{3} = \frac{18}{3} \quad x = 6$$



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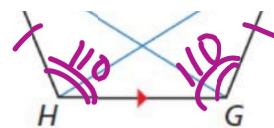
If  $\underline{EG = FH}$ , is trapezoid  $EFGH$  isosceles?

If  $m\angle HEF = 70^\circ$  and  $m\angle EGH = 110^\circ$



If  $m\angle H = 70^\circ$  and  $m\angle G = 110^\circ$ ,  
is trapezoid  $EFGH$  isosceles?

yes



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In trapezoid  $JKLM$ ,  $\angle J$  and  $\angle M$  are right angles, and  $JK = 9$

centimeters. The length of midsegment  $\overline{NP}$  of trapezoid  $JKLM$  is 12 centimeters. Sketch trapezoid  $JKLM$  and its midsegment. Find  $ML$ .

Handwritten work for finding  $ML$ :

$$\frac{x+9}{2} = 12$$

$$24 = x+9$$

$$-9 \quad -9$$

$$15 = x$$

$x = 15$

Handwritten work for finding  $ML$ :

$$12 = \frac{1}{2}(9+x)$$

$$12 = 4.5 + 0.5x$$

$$-4.5 \quad -4.5$$

$$7.5 = 0.5x$$

$$\frac{7.5}{0.5} = \frac{0.5x}{0.5}$$



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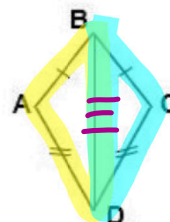
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If a quadrilateral is a kite, it has one diagonal forming two congruent triangles.

Given: kite  $ABCD$

Prove:  $\triangle BAD \cong \triangle BCD$

Proof:



Statements	Reasons
1. kite $ABCD$	1. <u>Given</u>
2. $\overline{AD} \cong \overline{CD}$ ; $\overline{AB} \cong \overline{CB}$	2. A kite has two distinct sets of adjacent, congruent sides.
3. $\overline{BD} = \overline{BD}$	3. Reflexive property.



4.  $\triangle BAD \cong \triangle BCD$

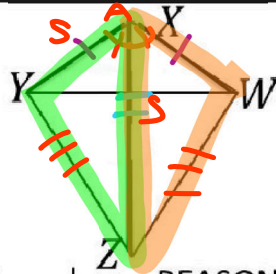
4. SSS



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Given:  $\overline{YX} \cong \overline{WX}$   
 $\overline{XZ}$  bisects  $\angle YXW$   
 Prove:  $\overline{YZ} \cong \overline{WZ}$



SAS  
 SSS  
 ASA  
 AAS

STATEMENT	REASON
1. $\overline{YX} \cong \overline{WX}$	1. <u>Given</u>
2. $\overline{XZ}$ bisects $\angle YXW$	2. Definition of bisector
3. $\angle YXZ \cong \angle WXZ$	3. <u>Reflexive Prop</u>
4. $\triangle YXZ \cong \triangle WXZ$	4. <u>SAS</u>
5. $\overline{YZ} \cong \overline{WZ}$	5. <u>CPCTC</u>



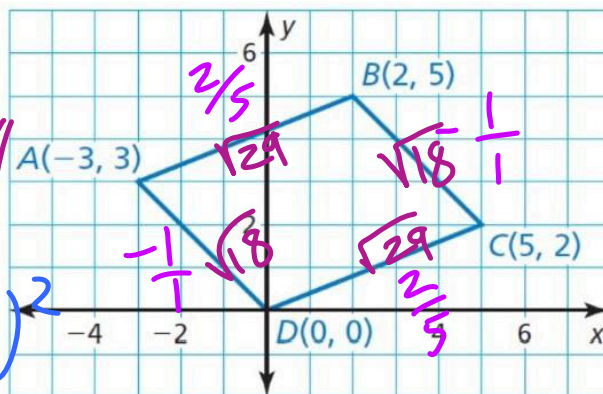
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Show that quadrilateral  $ABCD$  is a parallelogram.

$$\frac{y_2 - y_1}{x_2 - x_1} \text{ opp side //}$$

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



opp  
 sides //



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Find the length of midsegment  $\overline{YZ}$  in trapezoid  $STUV$ .

Midpoint  
 $ST \therefore VU$

$$\frac{x_1 + x_2}{2} \quad \frac{y_1 + y_2}{2}$$

$$\begin{matrix} (4, 8) & (7, 2) \\ x_1 & x_2 \\ y_1 & y_2 \end{matrix}$$

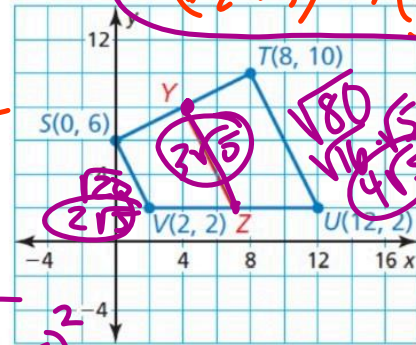
$$\sqrt{45}$$

$$\sqrt{9 \cdot 5}$$

$$\sqrt{(7-4)^2 + (2-8)^2}$$

$$\sqrt{3^2 + (-6)^2}$$

$$\sqrt{9 + 36}$$



$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\sqrt{9} =$$

$$\frac{2\sqrt{5} + 4\sqrt{5}}{2} = \frac{6\sqrt{5}}{2}$$

$$\frac{6\sqrt{5}}{2}$$



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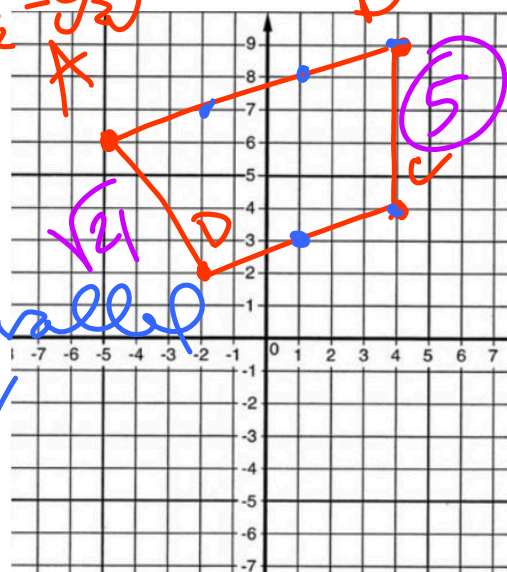
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The points  $A(-5, 6)$ ,  $B(4, 9)$ ,  $C(4, 4)$ , and  $D(-2, 2)$  form the vertices of a quadrilateral. Show that  $ABCD$  is a trapezoid. Then decide whether it is isosceles.

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Slopes  
 $AB \therefore DC$

$$\frac{1}{3} = \frac{1}{3} \text{ parallel}$$



$$\overline{AD} \sqrt{2}$$

$$\overline{BC} = 5$$

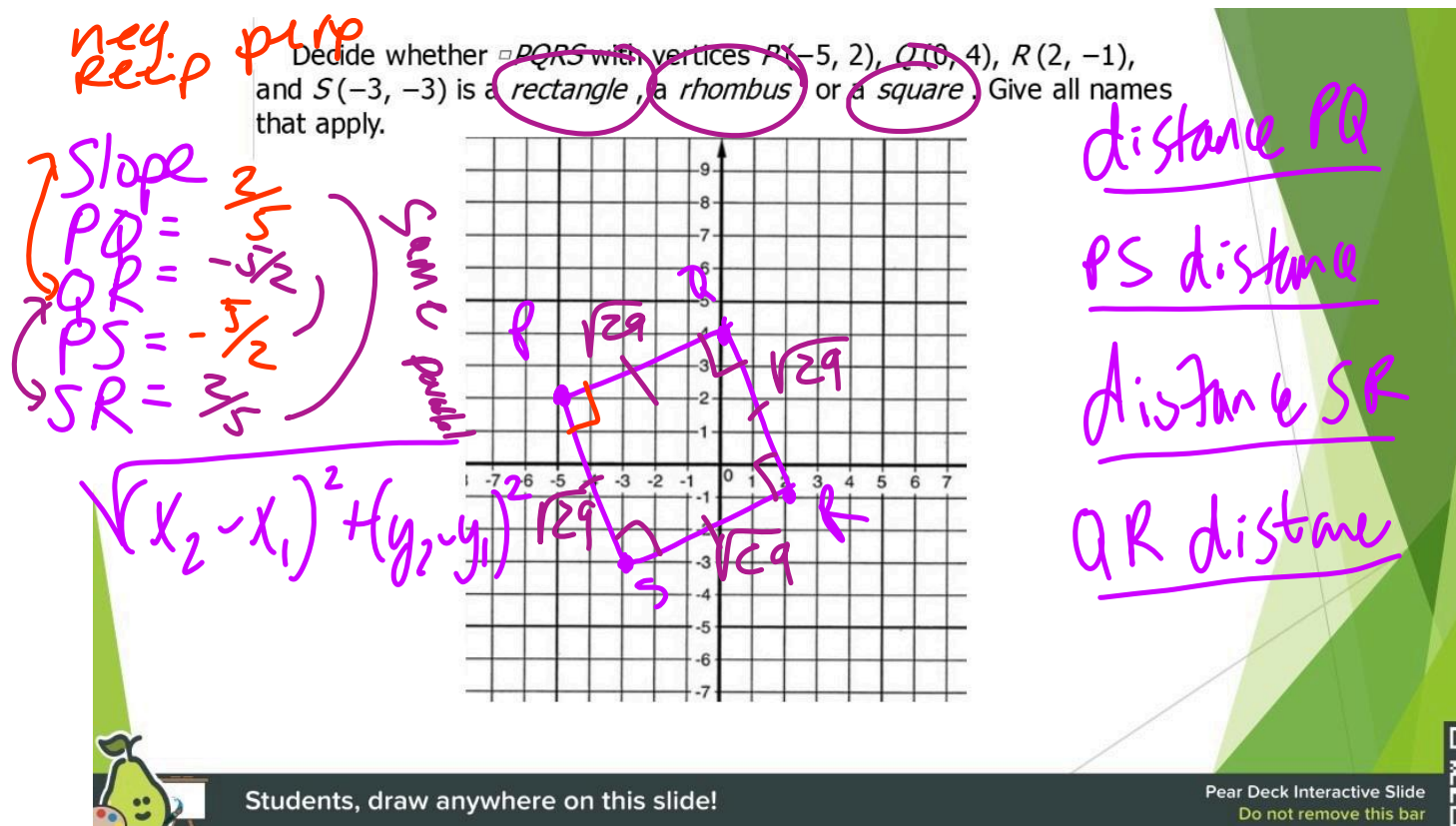
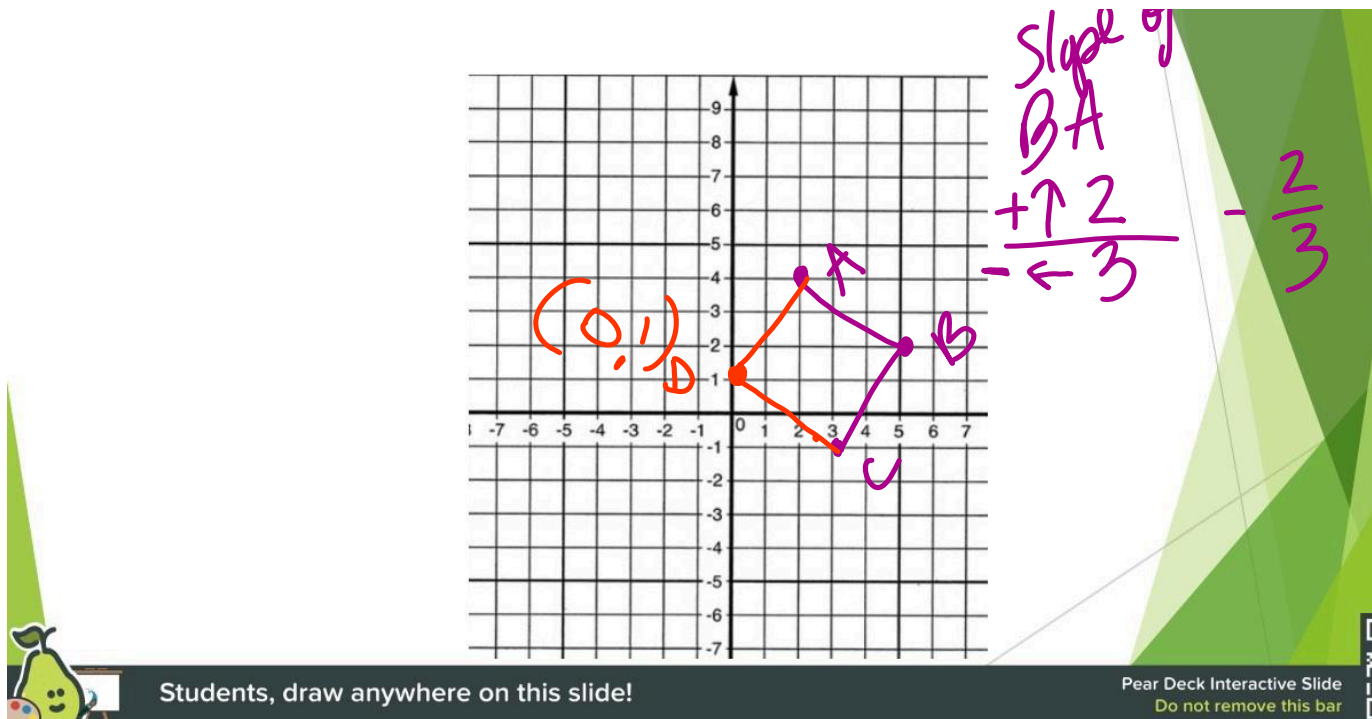
NOT  
ISOSCELES



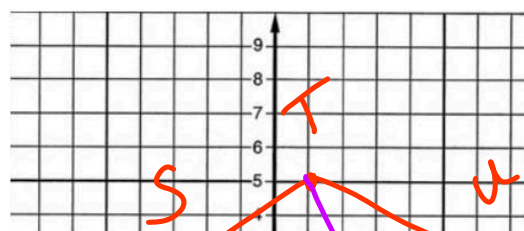
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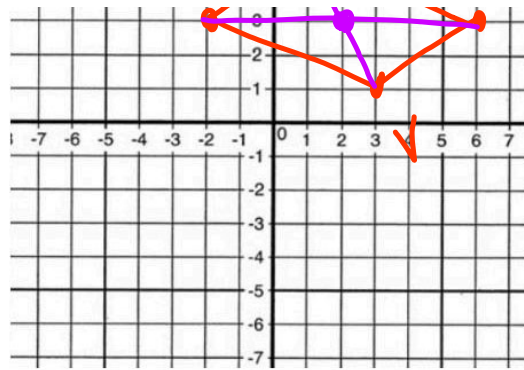
Three vertices of  $\square ABCD$  are  $A(2, 4)$ ,  $B(5, 2)$ , and  $C(3, -1)$ . Find the coordinates of vertex  $D$ .



Find the coordinates of the intersection of the diagonals of  $\square STUV$  with vertices  $S(-2, 3)$ ,  $T(1, 5)$ ,  $U(6, 3)$ , and  $V(3, 1)$ .







(2, 2)



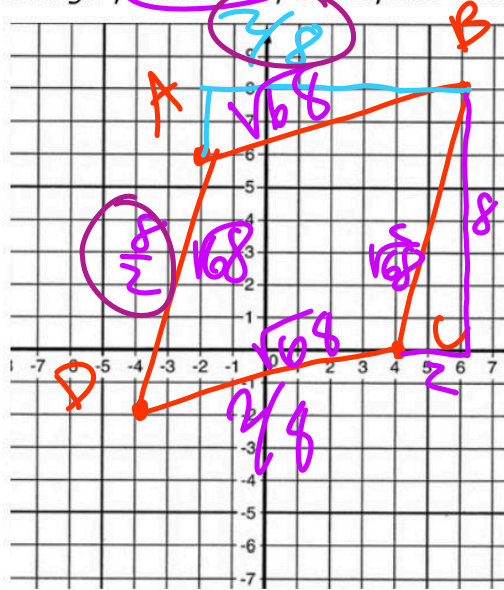
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Decide whether  $\square ABCD$  with vertices  $A(-2, 6)$ ,  $B(6, 8)$ ,  $C(4, 0)$ , and  $D(-4, -2)$  is a rectangle, a rhombus, or a square. Give all names that apply.

$$\begin{aligned} 2^2 + 8^2 &= c^2 \\ 4 + 64 &= c^2 \\ 68 &= c^2 \\ \sqrt{68} &= c \end{aligned}$$

not-recip.  
No Right  $\angle$ 's



$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\begin{aligned} 8^2 + 2^2 &= c^2 \\ 64 + 4 &= c^2 \\ 68 &= \sqrt{68} \end{aligned}$$



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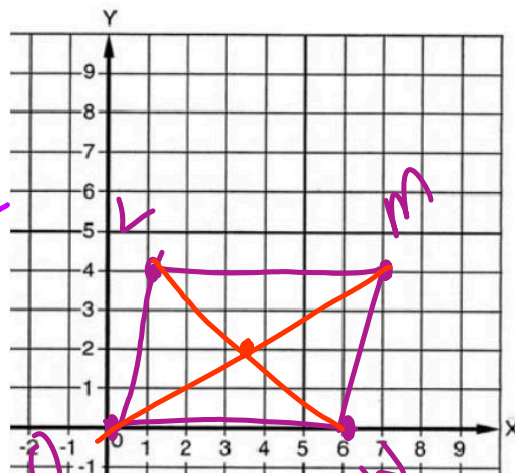
Find the coordinates of the intersection of the diagonals of  $\square LMNO$  with vertices  $L(1, 4)$ ,  $M(7, 4)$ ,  $N(6, 0)$ , and  $O(0, 0)$ .

A

$$y = \frac{4}{7}x$$

$$y = -\frac{4}{5}x + b$$

$$0 = -\frac{4}{5}(6) + b$$



(3.5, 2)

$$\begin{aligned} \frac{4}{7}x &= -\frac{4}{5}x + 4.8 \\ \frac{4}{7}x + \frac{4}{5}x &= 4.8 \end{aligned}$$

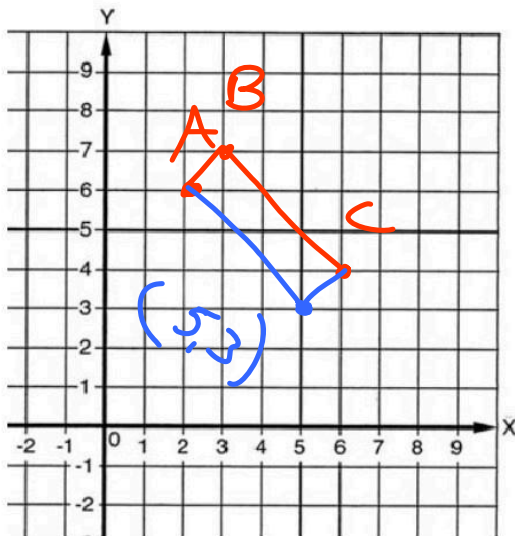


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### Check

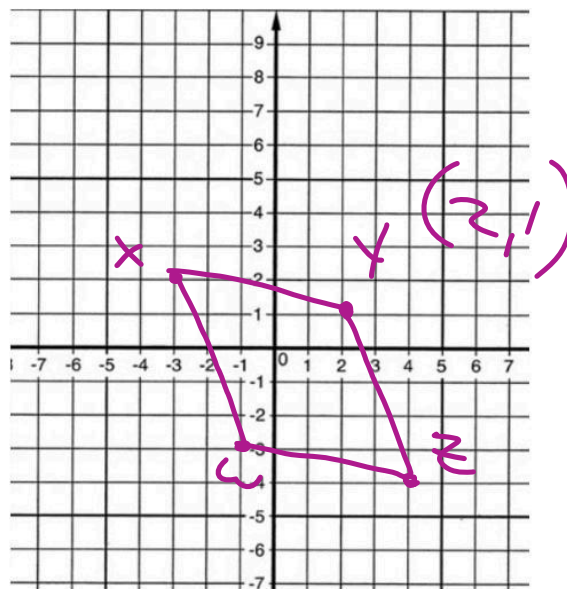
A quadrilateral has vertices  $A(2, 6)$ ,  $B(3, 7)$ , and  $C(6, 4)$ . Which of the following points would make  $ABCD$  a rectangle?



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Three vertices of  $\square WXYZ$  are  $W(-1, -3)$ ,  $X(-3, 2)$ , and  $Z(4, -4)$ . Find the coordinates of vertex  $Y$ .

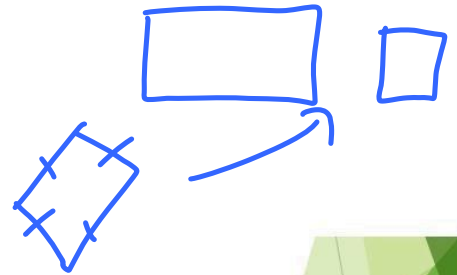


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Which statements are *true*, and which are *false*?

1. All parallelograms are quadrilaterals. T
2. No rhombus is a parallelogram. F
3. All squares are rhombi. T
4. Some rectangles are squares. T
5. Some rhombi are rectangles. T



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Answer *true* or *false*.

1. All rectangles are parallelograms. T
2. All squares are rectangles. T
3. All rhombi are squares. F
4. All squares are parallelograms. T
5. All rhombi are parallelograms. T



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