

Lesson 6.1 Factoring

Thursday, February 20, 2025 7:46 PM

Click the link below for the interactive Pear Deck PowerPoint

<https://app.peardeck.com/student/tuuyqgdye>

From

<<https://app.peardeck.com/presenter/tuuyqgdye/projector?returnTo=powerpoint>>



MCA Lesson
6.1 factoring



Factoring and Solving Equations



6.1 Factoring Polynomials with Common Factors

What You Will Learn

- Find the greatest common factor of two or more

expressions.

- ▶ Factor out the greatest common monomials factor from polynomials.
- ▶ Factor polynomials by grouping.

Copyright © 2019 Cengage Learning. All rights reserved.

2

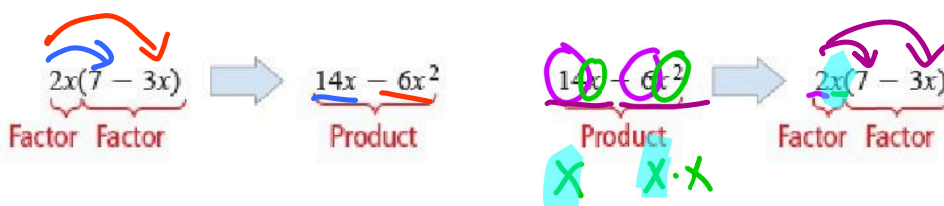
Greatest Common Factor

You have used the Distributive Property to multiply polynomials.

In this chapter, you will study the *reverse* process, which is **factoring**.

Multiplying Polynomials

Factoring Polynomials



3

Example 1 – Finding the Greatest Common Factor

Find the greatest common factor of $5x^2y^2$ and $30x^3y$, first factor each term.

$$5x^2y^2 \quad (14 \div 14 = 1) \quad (6 \div 2 = 3)$$

$$8x^5, 20x^3, 16x^4$$

Find the greatest common factor of $8x^5$, $20x^3$, and $16x^4$, first factor each term.

$$4x^3$$

Factor out the greatest common monomial factor from $6x - 18$

$$3(2x - 6)$$

Copyright © 2019 Cengage Learning. All rights reserved.

4

Example 4 – Greatest Common Monomial Factor

Factor out the greatest common monomial factor from $10y^3 - 25y^2$.

$$5y^2(2y - 5)$$

Factor out the greatest common monomial factor from $45x^3 - 15x^2 - 15$.

$$15(3x^3 - x^2 - 1)$$

Factor out the greatest common monomial factor from

$$3xy^2 - 15x^2y + 12xy$$

$$3xy(y - 5x + 4)$$

Copyright © 2019 Cengage Learning. All rights reserved.

5

Example 7 – Greatest Common Monomial Factor

Factor out the greatest common monomial factor from

$$35y^3 - 7y^2 - 14y.$$

$$7y(5y^2 - y - 2)$$

Factor the polynomial $-2x^2 + 8x - 12$

$$-2(x^2 - 4x + 6)$$

Example 9 – Common Binomial Factors

Factor each expression.

a. $5x^2(7x - 1) - 3(7x - 1)$

$$(5x^2 - 3)(7x - 1)$$

b. $2x(3x - 4) + 1(3x - 4)$

$$(2x + 1)(3x - 4)$$

c. $3y^2(y - 3) + 4(3 - y)$

$$(3y^2 + 4)(-y + 3)$$

Factoring by Grouping 2

But suppose you *group* the first two terms together and the last two terms together.

$$x^3 + 2x^2 + 3x + 6 = (x^3 + 2x^2) + (3x + 6) \quad \text{Group terms.}$$

$$x^2(x+2) + 3(x+2)$$

$$(x^2 + 3)(x + 2)$$

Copyright © 2019 Cengage Learning. All rights reserved.

8

Example 10 – Factoring by Grouping

Factor $x^3 + 2x^2 + x + 2$.

$$x^3 + x \quad 2x^2 + 2$$

$$x(x^2 + 1) + 2(x^2 + 1)$$

$$(x+2)(x^2 + 1)$$

Factor $3x^2 - 12x - 5x + 20$.

$$3x(x - 4) - 5(x - 4)$$

$$(3x - 5)(x - 4)$$

Copyright © 2019 Cengage Learning. All rights reserved.

9

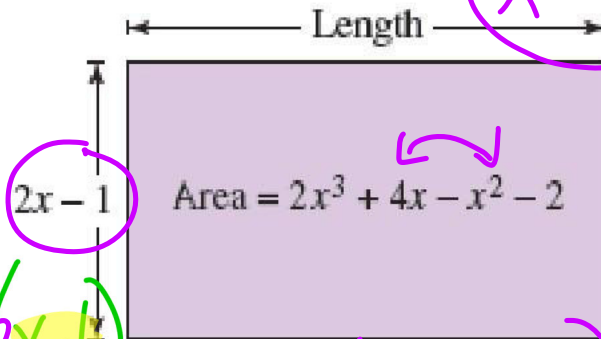
Example 12 – Geometry: Area of a Rectangle

The area of a rectangle of width $(2x - 1)$ feet is $(2x^3 + 4x - x^2 - 2)$ square feet, as shown below. Factor this expression to determine the length of the rectangle.

$$2x^3 - x^2 + 4x - 2$$

$$x^2(2x - 1)$$

$$2(2x - 1)$$



$$x^2 + 2$$

$$(x^2 + 2)(2x - 1)$$