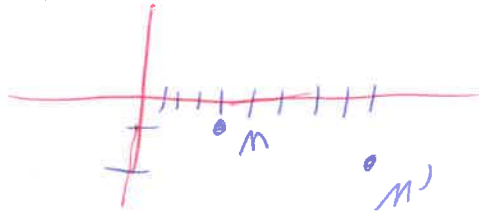


## Midterm Review

1. Point  $M(4, -1)$  is translated to  $M'(9, -2)$ . Which translation rule describes this movement?

$$\begin{array}{c} x \\ 4 + \square = 9 \\ \textcircled{5} \end{array}$$

$$\begin{array}{c} y \\ -1 + \square = -2 \\ \textcircled{-1} \end{array}$$



$$(x+5, y-1)$$

2.

Find the values of  $x$ ,  $ID$ , and  $MD$ . List your answers in order from least to greatest with commas separating your answers. \* (3 Points)

Given  $I$  is the midpoint of  $\overline{MD}$ , find  $x$ ,  $ID$ , and  $MD$ .



$$\begin{array}{r} 5x + 1 = 9x - 7 \\ -5x \quad -5x \\ \hline \end{array}$$

$$\begin{array}{r} 1 = 4x - 7 \\ +7 \quad +7 \\ \hline \end{array}$$

$$\begin{array}{r} 8 = 4x \\ 4 \quad 4 \\ \hline \end{array}$$


$$\textcircled{2 = x}$$

$$\boxed{x = 2}$$

$$ID = 11$$

$$MD = 11 + 11 = \underline{\underline{22}}$$

3.)

Given:  (with initial point A)

1. $AP : PB = 3 : 2$	<input checked="" type="radio"/> TRUE	<input type="radio"/> FALSE
2. $AP : AB = 2 : 5$	<input type="radio"/> TRUE	<input checked="" type="radio"/> FALSE
3. $PB : AB = 2 : 5$	<input checked="" type="radio"/> TRUE	<input type="radio"/> FALSE
4. $BP : PA = 2 : 3$	<input checked="" type="radio"/> TRUE	<input type="radio"/> FALSE
5. $AB : AP = 5 : 3$	<input checked="" type="radio"/> TRUE	<input type="radio"/> FALSE

4.)

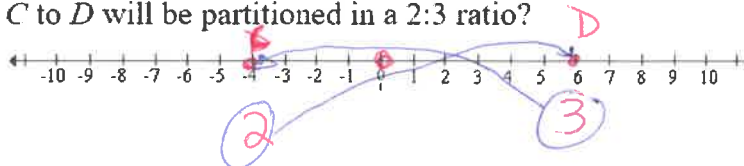
A line segment partitioned by a ratio of 3:4 can be thought of as having 7 congruent sections.

$$(3+4 = \underline{7})$$



5.)

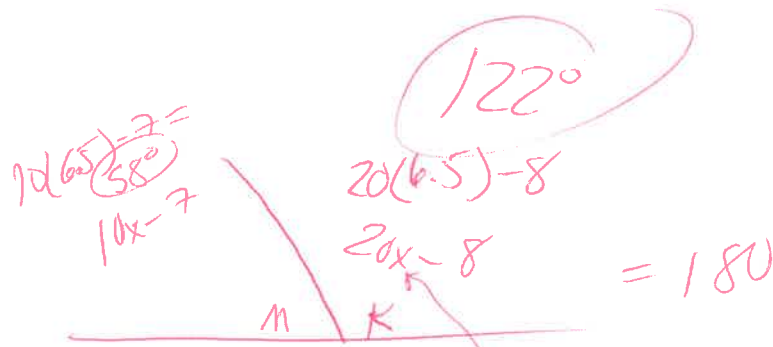
On a number line, point C is located at -4 and point D is located at 6. At what point must P be located so that the directed line segment from C to D will be partitioned in a 2:3 ratio?



$$\begin{array}{r} (3)(-4) + (2)(6) \\ -12 + 12 \end{array}$$

Total parts 2 + 3

$$= \frac{0}{5} = 0$$



6.)

$\angle M$  and  $\angle K$  are a linear pair. If  $m\angle M = 10x - 7$  and  $m\angle K = 20x - 8$ , find  $x$ . Find the measure of  $\angle K$ .

$$\begin{aligned}
 10x - 7 + 20x - 8 &= 180 \\
 30x - 15 &= 180 \\
 30x &= 195 \\
 x &= 6.5
 \end{aligned}$$

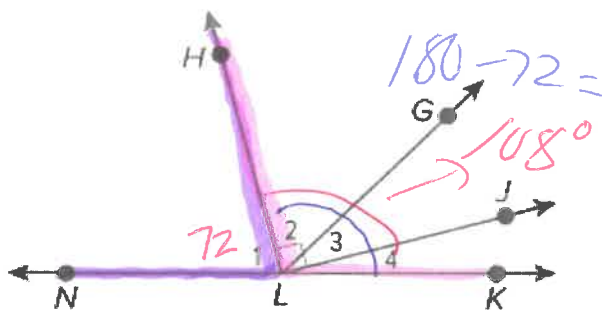
$$\begin{aligned}
 20(6.5) - 8 \\
 122^\circ
 \end{aligned}$$

$$x = 6.5$$

7.)  $\angle NLH = 72$  degrees

What is the measure of  $\angle KLH$ ?

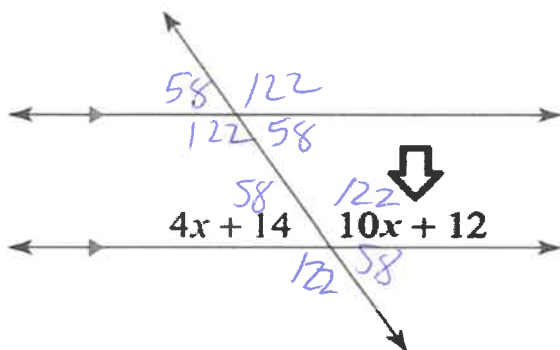
What kind of angles are they?



$$108^\circ$$

linear pair  
adjacent  
supplementary  
 $180^\circ$

8.)



Find the measures of all the angles.

What is the value of X?

$$4x + 14 + 10x + 12 = 180$$

$$14x + 26 = 180$$

$$14x = 154$$

$$x = 11$$

What is the measure of the angle with the arrow pointing at it?

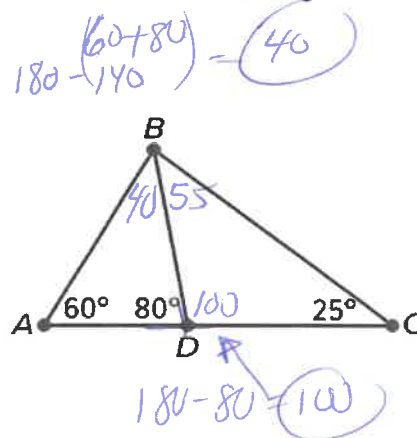
$$10(11) + 12 = 122^\circ$$

What is the measure of the angle that is marked, but does not have an arrow pointing at it?

$$4(11) + 14 = 58^\circ$$

9.)

Find the measure of  $\angle ABD$   $40^\circ$   
 Find the measure of  $\angle BDC$   $100^\circ$   
 Find the measure of  $\angle DBC$   $55^\circ$

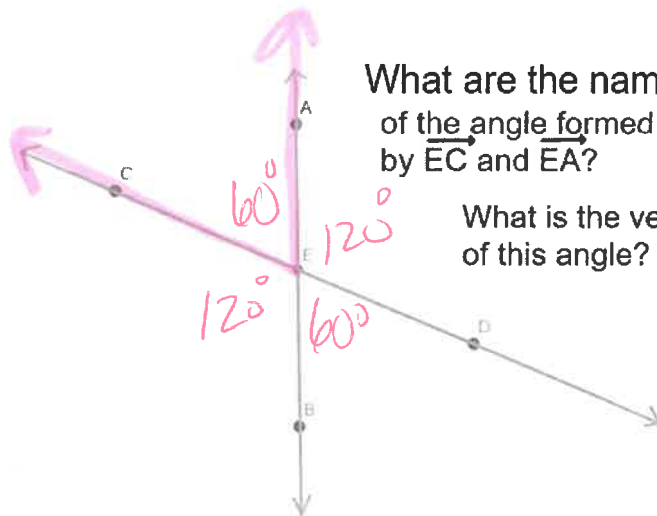


$$180 - (60 + 80) = 40$$

$$180 - (100 + 25) = 55$$

$$180 - 80 = 100$$

10.)



What are the names of the angle formed by  $\overrightarrow{EC}$  and  $\overrightarrow{EA}$ ?

$\angle AEC$  or  $\angle CEA$

What is the vertex of this angle?

Point E

What kind of angle is it? Obtuse, Acute, Right?

Name a pair of vertical angles.

$\angle CEA \cong \angle BED$  or  $\angle CEB \cong \angle AED$

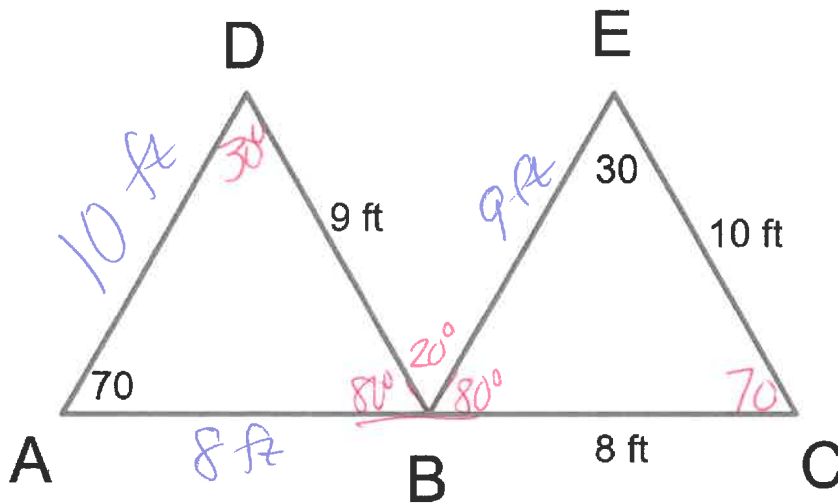
If  $\angle CEB = 120$  degrees find the remaining angles and justify your answers.

$\angle AED \cong \angle CEB$  are vertical  $\angle$ 's  $\neq 120$   
 $\angle AED \cong \angle DEB$  are a linear pair (180)  
 so  $180 - 120 = 60^\circ$

$\angle BED \cong \angle CEA$  are vertical angles  $= 60^\circ$

11.)

Triangle  $\overline{ADB}$  = Triangle  $\overline{CEB}$



$$180 - (30 + 70)$$

$$180 - 100 =$$

$$(80^\circ)$$

$$180 - (80 + 80) =$$

$$180 - 160 = 20^\circ$$

Determine the measures of  $\angle ADB$ ,  $\angle ABD$ ,  $\angle EBC$ ,  $\angle DBE$ ,  $\angle ECB$ ,  $\angle DBC$ ,  $\angle EBA$

$$30^\circ \quad 80^\circ \quad 80^\circ \quad 20^\circ \quad 70^\circ \quad 100^\circ \quad 100^\circ$$

$$(20 + 80) \quad (20 + 80)$$

Determine the length of AD, AC, and EB

$$\overline{AD} = \overline{CE}$$

$$10 \text{ ft}$$

$$\overline{EB} = \overline{ED}$$

$$9 \text{ ft}$$

$$\overline{AB} = \overline{CB}$$

$$8 \text{ ft}$$

$$\overline{AC} =$$

$$8 \text{ ft} + 8 \text{ ft} = 16 \text{ ft}$$

$$\overline{AB} + \overline{BC}$$

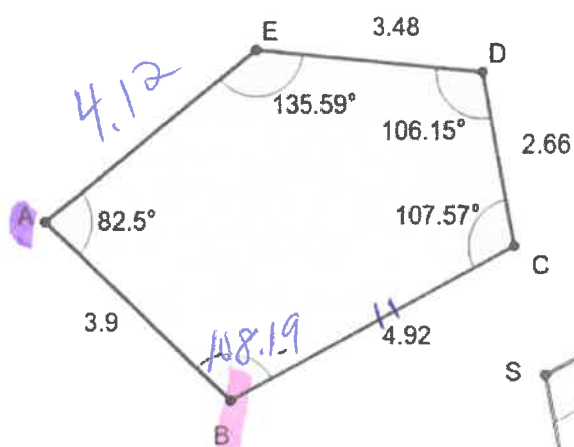
12.)

$$\underline{ABCDE} = \underline{MHWSV}$$

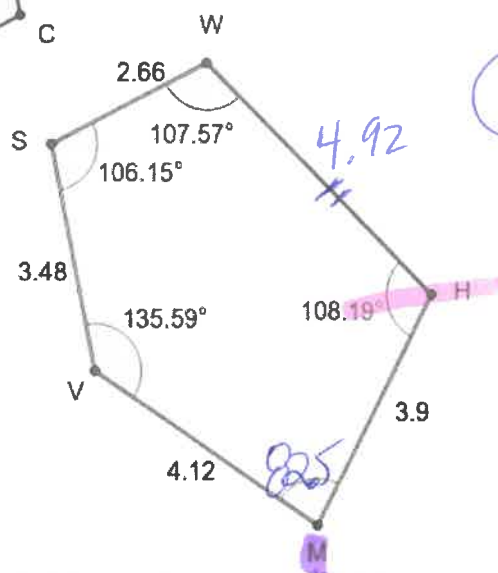
Determine the measure of  $\angle M$  and  $\angle B$

$82.5^\circ$

$108.19$

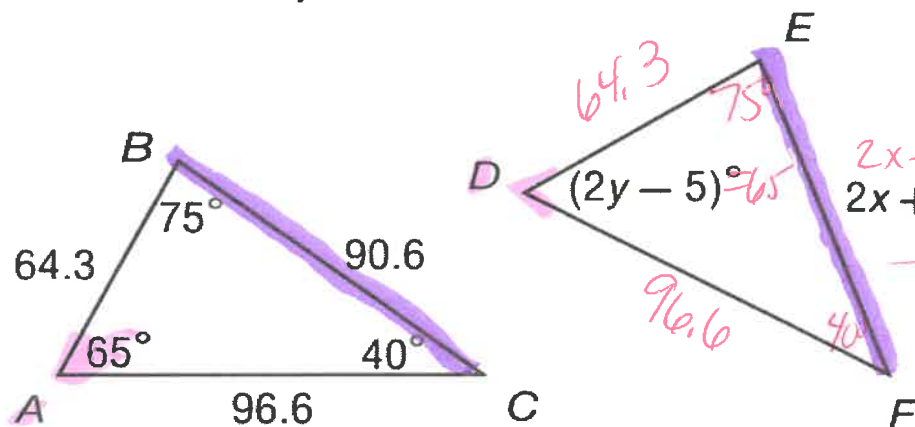


What is the side length of WH and AE?



$\overline{BC} = \overline{MV}$   
 $4.92 = 4.12$

- 13.) In the diagram,  $\triangle ABC \cong \triangle DEF$ . Find the values of  $x$  and  $y$ .



$$\frac{2y - 5}{+5} = \frac{65}{+5}$$

$$\frac{2y}{2} = \frac{20}{2}$$

$$y = 35$$

$$2x + 35 = 90.6$$

$$2x + y = 35$$

$$\frac{2x}{2} = \frac{55.6}{2}$$

$$x = 27.8$$

Find the length of side EF: 90.6

Find the length of side DE: 64.3

Find the measure of  $\angle D$ : 65°

Find the measure of  $\angle F$ : 40°

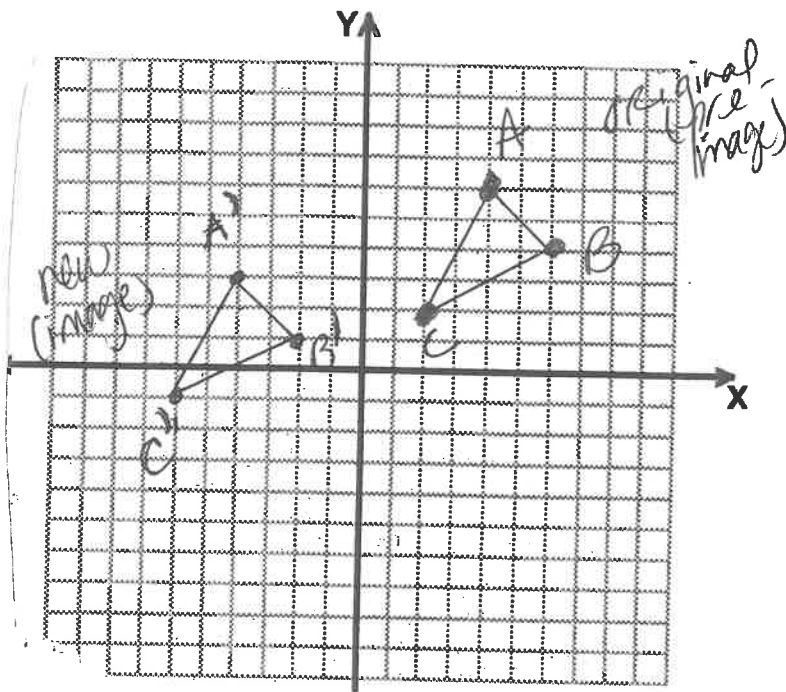


14.) What is the transformation that maps ABC on to A'B'C'?

— Part A

\*Include the rule of the transformation.

What transformation will map ABC back on to itself? — Part B



Part A

$$(x-8, y-3)$$

(8 left : 3 down  
translation

Part B

360° Rotation

15.)

Draw a reflection of Pentagon SUDHE over the y-axis.

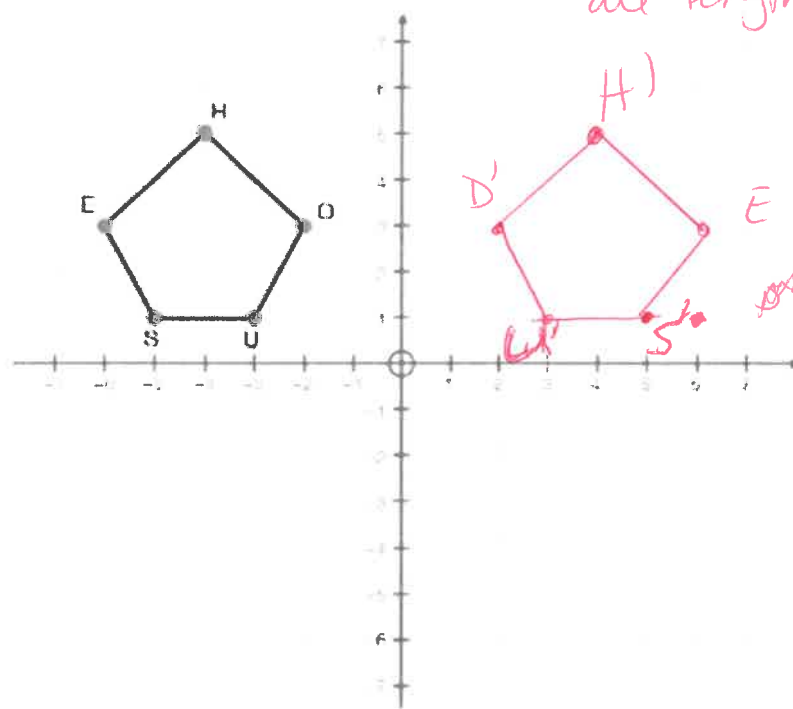
Is this transformation rigid motion? *yes*

What is the length of S'U' after the reflection? *2 units*

What do you know about all the lengths of the new image?

*all lengths stay same*

*Rigid Motion preserves distance*



))

$$A(1, 2) \quad B(3, -1) \quad C(7, 6)$$

$$AB \quad \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\sqrt{(3 - 1)^2 + (-1 - 2)^2}$$

$$\sqrt{2^2 + (-3)^2}$$

$$\sqrt{4 + 9}$$

$$\sqrt{13}$$

$$BC \quad \sqrt{(7 - 3)^2 + (6 - (-1))^2}$$

$$\sqrt{4^2 + 7^2}$$

$$\sqrt{16 + 49}$$

$$\sqrt{65}$$

$$AC \quad \sqrt{(7 - 1)^2 + (6 - 2)^2}$$

$$\sqrt{6^2 + 4^2}$$

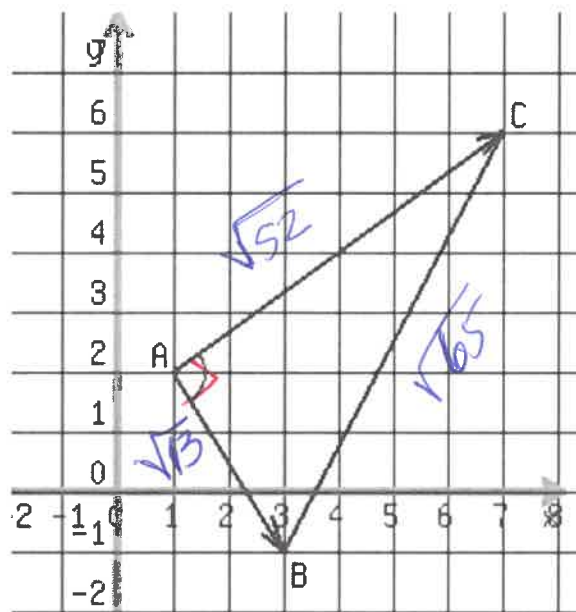
$$\sqrt{36 + 16}$$

$$\sqrt{52}$$

16.)

Is triangle ABC a right triangle?  
Justify your answer.

Determine the area of the triangle.  
Determine the perimeter of the triangle.



AC slope =  $\frac{2}{3}$   
AB slope =  $-\frac{3}{2}$   
perpendicular  
lines  
negative  
(opposite)  
reciprocals  
Right  $\angle$

Perimeter:

$$\sqrt{13} + \sqrt{65} + \sqrt{52} = 18.9$$

Area:

$$\frac{1}{2}bh \quad \frac{1}{2}(\sqrt{13})(\sqrt{52}) = 13$$

17.) Consider the statement: If the sum of two angles is  $180^\circ$  then the angles are supplementary. Determine if it is a True or False statement.

$P \rightarrow Q$

True

A) Converse:

$Q \rightarrow P$

If Angles are supplementary then they equal  $180^\circ$

True

B) Inverse:

$\neg P \rightarrow \neg Q$

If 2 angles are NOT  $180^\circ$  then they are NOT Supp.

True

C) Contrapositive:

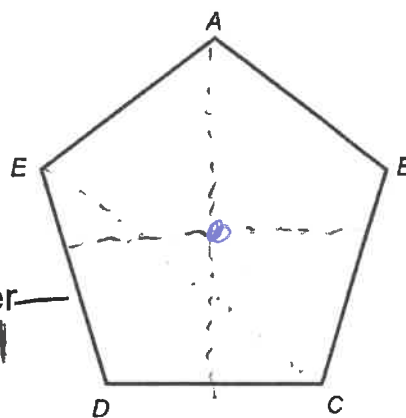
$\neg Q \rightarrow \neg P$

If 2 angles are NOT Supp. then they are NOT NOT  $180^\circ$

18.)

Which transformations would map the pentagon on to itself?

- a.) 180 degrees rotation about the center
- ☒ b.) 360 degrees rotation about the center
- c.) reflection of a horizontal line through the center
- ☒ d.) reflection of a vertical line through the center
- e.) reflection of a diagonal from point E to C

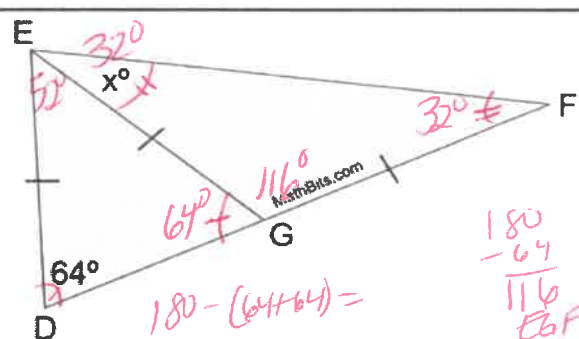


19.)

$\triangle DEG$  and  $\triangle EGF$  are isosceles.

$m\angle EDG = 64^\circ$

Find  $m\angle GEF$ .  $32^\circ$



$$180 - 116 = 64 \div 2 = 32$$

Find  $\angle EGF$  and  $\angle GFE$  and  $\angle DGE$  and  $\angle GED$

$116^\circ$

$32^\circ$

$64^\circ$

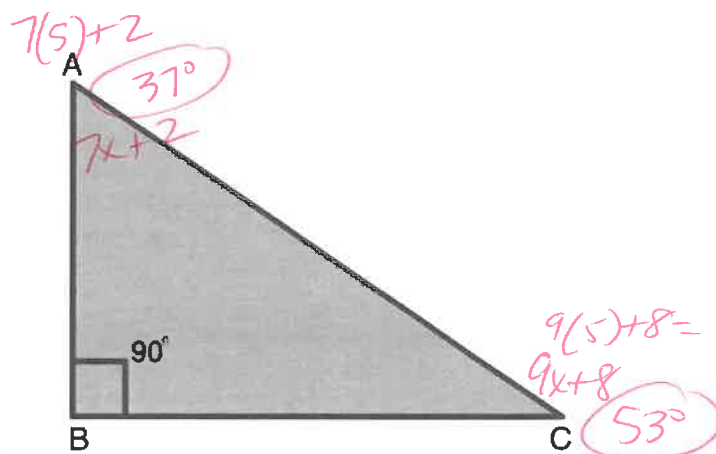
$52^\circ$

20.)

$\angle BAC$  measure is  $7x+2$

and  $\angle ACB$  is  $9x+8$

Solve for  $x$  and find the degrees of both angles.



$$90 + 7x + 2 + 9x + 8 = 180$$

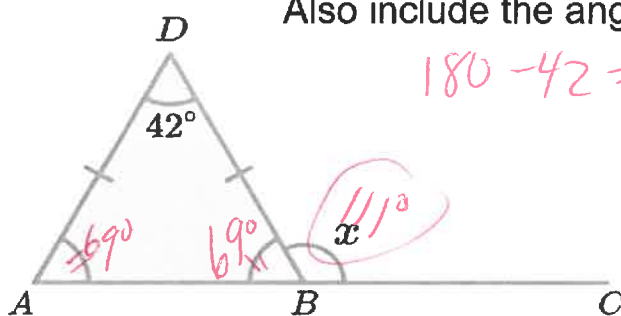
$$16x + 100 = 180$$

$$\begin{array}{r} 16x = 80 \\ \hline 16 \quad 16 \end{array}$$

$$(x = 5)$$

$$\begin{array}{r} \checkmark 90 \\ + 53 \\ + 37 \\ \hline 180 \checkmark \end{array}$$

21.) Determine the size of the exterior angle  $CBD$ , labelled  $x$ .



Also include the angle degrees for  $\angle DAB$  and  $\angle DBA$  first.

$$180 - 42 = \frac{138}{2} = 69^\circ$$

$$69 + 42 = x$$

$$111 = x$$

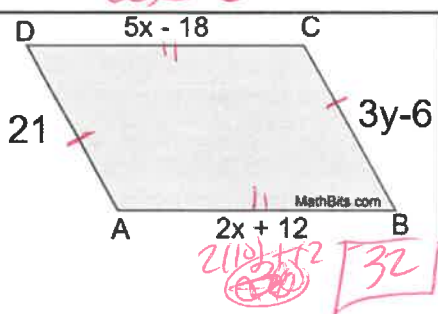
$$\text{or } 180 - 69 = 111^\circ$$

22.)

The sides of parallelogram  $ABCD$  are represented as shown.

Solve for  $x$  and  $y$ .

What is the length of  $AB$ ?



$$5(10) - 18 = 32$$

$$\checkmark (3 \cdot 9) - 6 = 21 \checkmark$$

$$\begin{array}{r} 21 = 3y - 6 \\ +6 \quad +6 \\ \hline 27 = 3y \end{array}$$

$$\frac{27}{3} = \frac{3y}{3}$$

$$9 = y$$

$$2(10) + 12 = 32$$

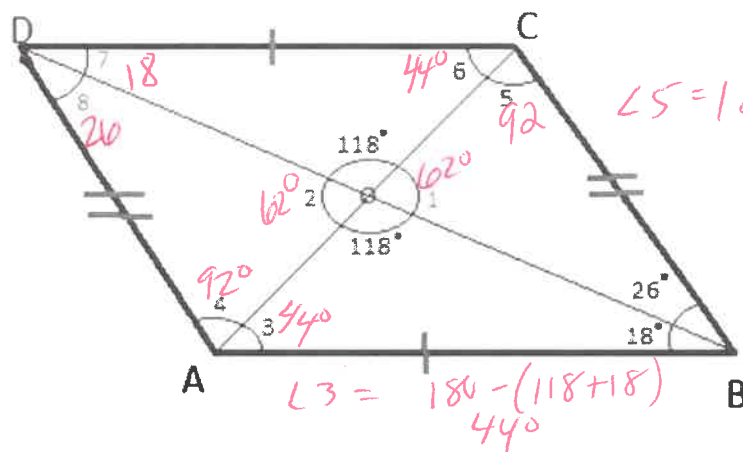
$$\begin{array}{r} 2x + 12 = 5x - 18 \\ -2x \quad -2x \\ \hline 12 = 3x - 18 \end{array}$$

$$\begin{array}{r} 12 = 3x - 18 \\ +18 \quad +18 \\ \hline 30 = 3x \end{array}$$

$$\frac{30}{3} = \frac{3x}{3}$$

$$x = 10$$

23.)



Solve for angles 1-8.

$\angle 3$  &  $\angle 6$  are Alternate Interior  $\angle$ 's so =  
BOTH  $44^\circ$

$\angle 4$  &  $\angle 5$  also Alt. Int.  $\angle$ 's so =  
 $92^\circ$

$\angle 7$  ALT INT with  $\angle ABD$  so =  $18^\circ$

$\angle 8$  ALT INT. with  $\angle CBD$  so =  $26^\circ$

## Vocab to know:

parallel, transversal, perpendicular,  
intersect, horizontal, vertical, diagonal, linear pair of angles,  
vertex, vertical angles, supplementary, complementary,  
midpoint, triangle sum theorem,  
exterior angle theorem, properties of parallelograms,  
obtuse/acute/right angles, corresponding, alternate  
interior, alternate exterior, consecutive interior,  
congruence, area, perimeter  
transformations: reflection/rotation/translation and rules -  
rigid motion  
converse, inverse, contrapositive  
isosceles and equilateral triangles  
Proofs/Properties