

Lesson 2.3 Two-Dimensional Figures

Tuesday, September 26, 2023 7:54 PM

Click Link Below to Open the Interactive Pear Deck PowerPoint

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Lesson 2.3
Two



Lesson 2.3 Two-Dimensional Figures

Workbook pages 81-90

MA.912.GR.3.4

Use coordinate geometry to solve mathematical and real-world problems on the coordinate plane involving perimeter or area of polygons.

MA.912.GR.4.4

Solve mathematical and real-world problems involving the area of two-dimensional figures.

Content Objective

Students model and find measures of two-dimensional objects.



Learn

Perimeter, Circumference, and Area



A **polygon** is a closed plane figure with at least three straight sides.

The **perimeter** of a polygon is the sum of the lengths of the sides of the polygon. Some shapes have special formulas for perimeter, but all are derived from the basic definition of perimeter.

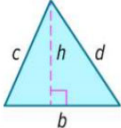
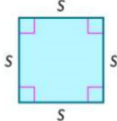
The **circumference** of a circle is the distance around the circle.

Area is the number of square units needed to cover a surface.

Learn

Perimeter, Circumference, and Area

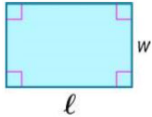
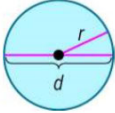


Perimeter, Circumference, and Area	
Triangle	Square
	
Perimeter $P = b + c + d$ Area $A = \frac{1}{2}bh$	Perimeter $P = s + s + s + s = 4s$ Area $A = s^2$

Learn

Perimeter, Circumference, and Area



Perimeter, Circumference, and Area	
Rectangle	Circle
	
Perimeter $P = \ell + w + \ell + w = 2\ell + 2w$ Area $A = \ell w$	Circumference $C = 2\pi r$ or $C = \pi d$ Area $A = \pi r^2$

Learn

Perimeter, Circumference, and Area



You can use the Distance Formula to find the perimeter and area of a polygon graphed on a coordinate plane. You can also use the Distance Formula to calculate the radius of a circle and then use the appropriate equations for circumference and area.

An **equilateral polygon** has all sides congruent. An **equiangular polygon** has all angles congruent. A **regular polygon** is a convex polygon that is both equilateral and equiangular.

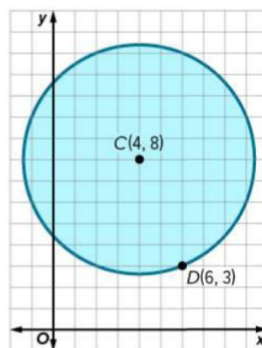
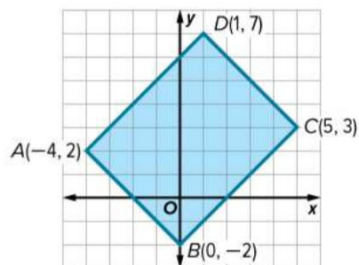
Example 1

Find Perimeter, Circumference, and Area

Find the perimeter or circumference and area of each figure.

a. Rectangle $ABCD$

b. Circle C

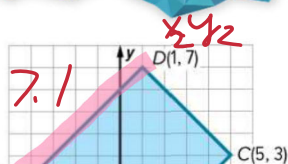


Example 1

Find Perimeter, Circumference, and Area

a. Rectangle $ABCD$

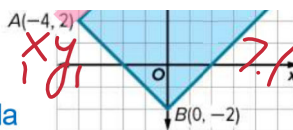
First, find the length ℓ of the rectangle by



using the Distance Formula. Let the length be equal to AD .

$$l = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \quad \text{Distance Formula}$$

$$\begin{aligned} &= \sqrt{(1 - (-4))^2 + (7 - 2)^2} \\ &= \sqrt{(5)^2 + (5)^2} \\ &= \sqrt{25 + 25} \\ &= \sqrt{50} \approx 7.1 \end{aligned}$$



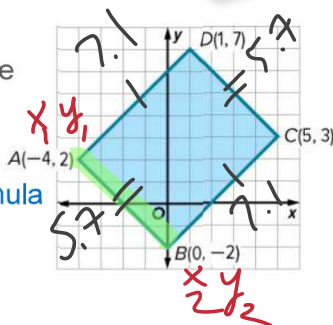
Example 1

Find Perimeter, Circumference, and Area

Next, find the width w of the rectangle by using the Distance Formula. Let the width be equal to AB .

$$w = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \quad \text{Distance Formula}$$

$$\begin{aligned} &= \sqrt{(0 - (-4))^2 + (-2 - 2)^2} \\ &= \sqrt{(4)^2 + (-4)^2} \\ &= \sqrt{16 + 16} \\ &= \sqrt{32} = 5.7 \end{aligned}$$



Example 1

Find Perimeter, Circumference, and Area

Use the length and width that you calculated to find the perimeter and area of the rectangle.

Perimeter of a rectangle

$$7.1 + 7.1 + 5.7 + 5.7$$
$$\textcircled{25.6}$$

Area of a rectangle

$$A = lw$$
$$A = (7.1)(5.7)$$
$$\textcircled{A = 40.5}$$

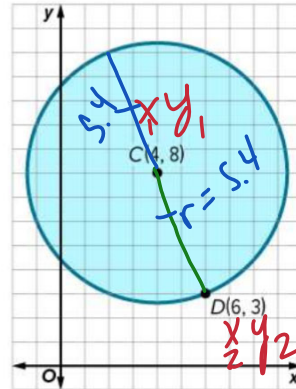
Example 1

Find Perimeter, Circumference, and Area

b. Circle C

Use the Distance Formula to calculate the length of the radius of the circle.

$$r = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \quad \text{Distance Formula}$$
$$\begin{aligned} & \sqrt{(6-4)^2 + (3-8)^2} \\ & \sqrt{2^2 + (-5)^2} \\ & \sqrt{4 + 25} \\ & \sqrt{29} = 5.4 \end{aligned}$$



diagonal
10.8

Example 1

Find Perimeter, Circumference, and Area

Use the value of r to find the circumference and area of the circle.

$$C = 2\pi r$$
$$C = 2(\pi)(5.4)$$
$$C = 33.9$$

Circumference

$$C = \pi d$$
$$C = 10.8\pi = 33.9$$

$$A = \pi r^2$$

Area of a circle

$$A = \pi (5.4)$$

$$A = 29.2(\pi)$$

$$A = 91.6$$

Example 1

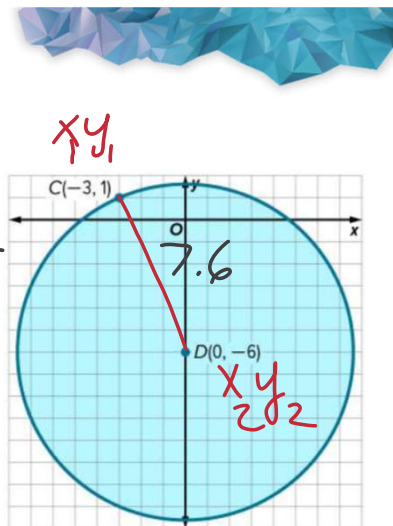
Find Perimeter, Circumference, and Area

Check

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Find the circumference and area of the circle. Round to the nearest tenth, if necessary.

$$\begin{aligned} & (0 + 3)^2 + (-6 - 1)^2 \\ & (3)^2 + (-7)^2 \\ & 9 + 49 \\ & \sqrt{58} = 7.6 \end{aligned}$$



$$\begin{aligned} A &= \pi r^2 \\ &= \pi (7.6)^2 \\ &= 181.5 \end{aligned}$$

$$\begin{aligned} C &= 2\pi r \\ &= 2(\pi)(7.6) \\ &= 47.8 \end{aligned}$$

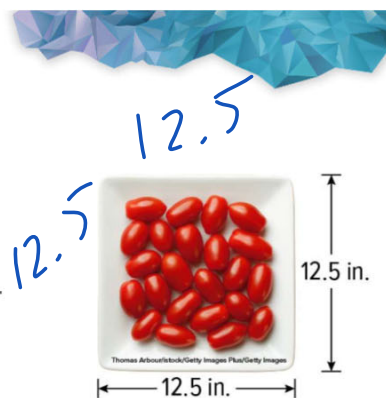
$$\begin{aligned} & \pi d \\ &= \pi (15.2) \end{aligned}$$

Example 2

Modeling with Two-Dimensional Figures

TABLEWARE Use an appropriate two-dimensional model and the dimensions provided in the image to calculate the perimeter and area of the serving platter.

$$12.5(4) = 50 \text{ in}$$



$$A = lw \\ (12.5)(12.5) \\ 156.25$$

Example 2

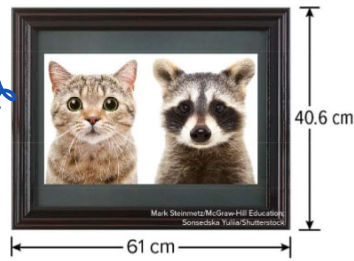
Modeling with Two-Dimensional Figures

Check

FRAMES Use an appropriate two-dimensional model and the dimensions provided in the image to calculate the perimeter and area of the framed art.

$$40.6 + 61 + 40.6 + 61 =$$

$$203.2$$



$$A = lw$$
$$(40.6)(61)$$
$$2476.6$$