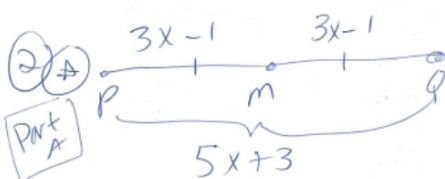


① congruent $\cong$ $\overline{BC} \cong \overline{DA}$ $\overline{AC}$
 1st blank 2nd blank 3rd blank

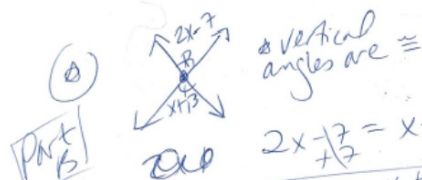


$$3x-1+3x-1=5x+3$$

$$6x-2=5x+3$$

$$\begin{array}{r} 6x-2=5x+3 \\ -5x \quad -2 \\ \hline 1x=5 \end{array}$$

$$x=5$$



$$2x-7=x+13$$

$$\begin{array}{r} 2x-7=x+13 \\ -x \quad -13 \\ \hline x=20 \end{array}$$

$$2(20)-7=33$$

$$20+13=33$$

$$180-33=147^\circ$$

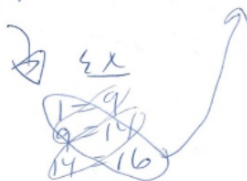
the other 2

Part C $\otimes$ Proof

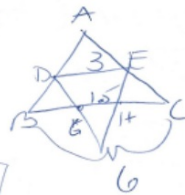
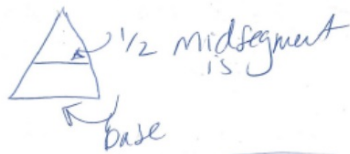
Reasons

- 1) Given
- 2) Corresponding angles $\cong$
- 3) Vertical angles are $\cong$
- 4) Corresponding angles are $\cong$
- 5) Transitive property

$$5) \angle 1 \cong \angle 16$$

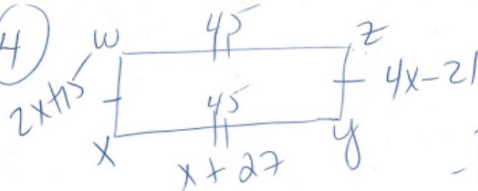


(3)



$$BC = 6$$

(4)



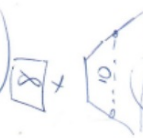
$$x = 18$$

$$18 + 27 = 45$$

$$\begin{array}{r} 2x + 15 = 4x - 21 \\ -2x \quad -2x \\ \hline 15 = 2x - 21 \\ +21 \quad +21 \\ \hline 36 = 2x \end{array}$$

$$\begin{array}{r} 15 = 2x - 21 \\ +21 \quad +21 \\ \hline 36 = 2x \end{array}$$

(5)



$$2 \cdot 10 = \frac{1}{2}(x + x + 4) \cdot 2$$

$$\begin{array}{r} 20 = (2x + 4) \\ 20 = 2x + 4 \\ -4 \quad -4 \\ \hline 16 = 2x \end{array}$$

$$\frac{16}{2} = \frac{2x}{2}$$

$$\begin{array}{l} x = 8 \text{ ft Part A} \\ \text{OR } 96 \text{ in} \\ x + 4 = 12 \text{ ft } 144 \text{ in} \\ 8 + 4 \end{array}$$

$$96 \div 3 = 32 + 1 \text{ corner} = 33$$

$$144 \div 3 = 48 + 1 \text{ corner} = 49$$

$$33 + 49 = 82$$

$$82 / 25 = 3.28$$

$$4 \text{ bags}$$

(6) $AB = ED$
 ~~$2x+7 = 4x+5$~~
 ~~$-2x -2x$~~
 ~~$7 = 2$~~

$$\begin{array}{r} 2x+7 = 5x-2 \\ -2x \quad -2x \\ \hline 7 = 3x-2 \\ +2 \quad +2 \\ \hline 9 = 3x \\ \frac{9}{3} = \frac{3x}{3} \quad \boxed{x=3} \end{array}$$

~~$2(3)+7$~~

$4\overset{EF}{(3)}+5 = \boxed{17}$

yes congruent ASA

(7) $\frac{4}{(5x-3)} \neq \frac{5}{(4x+3)}$ or $\frac{4}{5} \neq \frac{(5x-3)}{(4x+3)}$

cross multiply

$$\begin{array}{r} 4(4x+3) = 5(5x-3) \\ 16x+12 = 25x-15 \\ -16x \quad -16x \\ \hline 12 = 9x-15 \end{array}$$

$$\begin{array}{r} 12 = 9x-15 \\ +15 \quad +15 \\ \hline 27 = 9x \end{array}$$

$$\begin{array}{r} 27 = 9x \\ \frac{27}{9} = \frac{9x}{9} \\ \boxed{3 = x} \end{array}$$

Plug into $\overline{AC}$ $5+4(3)+3$
 $5+12+3 = \boxed{20}$

$$(8) \quad \frac{2}{7} + \frac{2}{1} = \frac{2}{7} + \frac{14}{7} = \frac{16}{7}$$

Point A $(\frac{16}{7}, -1)$

$$-4 + 2 = -2$$

Point B $(2, -\frac{14}{5})$

$$3 + 2 = 5$$

Point C $(5, 1)$

Part A

Part B

Rule

$(x, y) \rightarrow (x+2, y)$

(9) Part A: Point B
Part B: 90°
Part C: 270°

or reflection $x=1$
* know your rules
 $90^\circ \quad -y, x$
 $180^\circ \quad -x, -y$
 $270^\circ \quad y, -x$

(10) A $(-5, -1)$ $180^\circ (-x, -y)$
 A' $(5, 1)$ $A''(3, -2)$ $x-2, y-3$
 B $(-3, -1)$ $B''(1, -2)$
 B' $(3, 1)$
 C $(-2, -2)$ $C''(0, -1)$
 C' $(2, 2)$
 D $(-3, -4)$ $D''(1, 1)$
 D' $(3, 4)$

E $(-6, -3)$
 E' $(6, 3)$ $E''(4, 0)$
 F $(-4, -2)$
 F' $(4, 2)$
 F'' $(2, -1)$

(11) $A(2,4)$ $A'(-2,1)$ $(-x, y-3)$
 $B(4,2)$ $B'(-4,-1)$ Rule
 $C(0,0)$ $C''(0,-3)$
 $D(0,2)$ $D''(0,-1)$

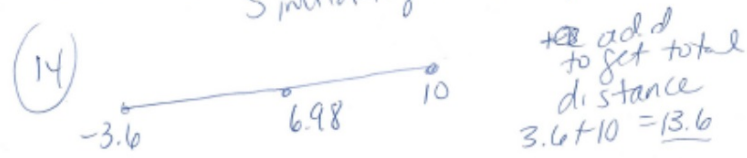
(12) Reflection & Translation
 180° Rotation & Translation



$\frac{1}{2} = \frac{3}{6}$ New original

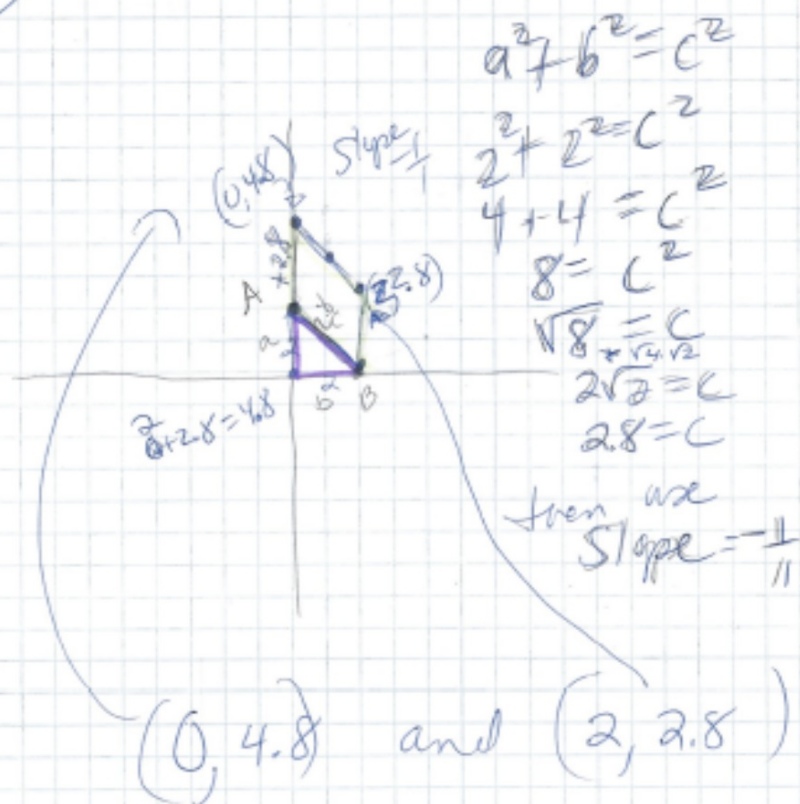
Part A - reduction
Dilation scale factor
 $k = \frac{1}{2}$
and Rotation
Part B
Similar AA or

Similarity AA, SSS, SAS



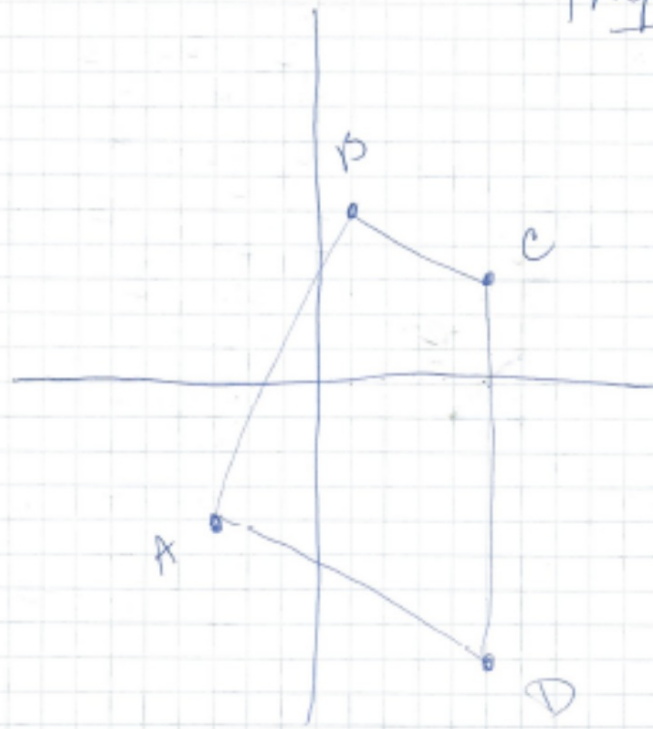
$\frac{2}{9}$ of the way
 $\frac{2}{9} \times 13.6 = 10.58$
 $-3.6 + 10.58 = 6.98$

#15



#16'

trapezoid



(17) see graph at the end too!

$$J \begin{pmatrix} 4 & 2 \\ x & y \end{pmatrix} \quad K \begin{pmatrix} 2 & 1 \\ x' & y' \end{pmatrix}$$

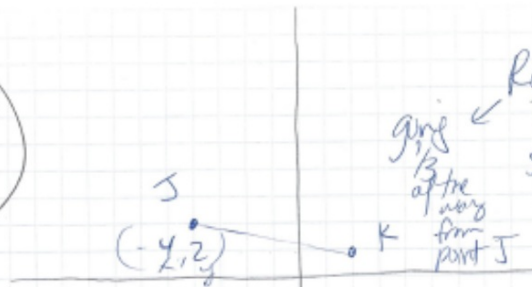
1:2
Ratio
total parts = 3

$$\begin{pmatrix} -4 & 2 \\ 1 & 2 \end{pmatrix} \quad \frac{-8+2}{3} = \frac{-6}{3} = -2$$

$$\begin{pmatrix} 4 & 4 \\ 2 & 1 \\ 1 & 2 \end{pmatrix} \quad \frac{1+4}{3} = \frac{5}{3}$$

$$\left(-2, \frac{5}{3} \right)$$

(17)



Ratio 1:2
Total parts = 3
Slope $-\frac{1}{6}$

$$\frac{y}{x} = \frac{-1 \cdot \frac{1}{3}}{6 \cdot \frac{1}{3} \text{ of the way}} = -\frac{1}{3} \text{ change in } y$$

$$\begin{pmatrix} x & y \\ -4 & 2 \\ +2 & +\frac{1}{3} \end{pmatrix} = \begin{pmatrix} 2 & \frac{7}{3} \\ -1 & -\frac{1}{3} \end{pmatrix}$$

$\left(-2, \frac{5}{3} \right)$ is your answer

(18)



look up pictures
on google of
cross-sections of
pentagonal pyramid

- Triangle
- Trapezoid
- Pentagon

(19)

1-D
linear/perimeter
 $\frac{1}{3}$

2-D
area (squared)
 $(\frac{1}{3})^2 = \frac{1}{9}$

3-D
Volume
(cubed)
 $(\frac{1}{3})^3 = \frac{1}{27}$

(20)



tube
also google
for picture to
help visualize

(2) Surface area

$$\left(\begin{array}{c} \square \\ 2.5 \end{array} \right)^3 \times 4 \text{ sides} + \left(\begin{array}{c} 2.5 \times 2.5 \\ \text{top} \end{array} \right) \times 4$$

Figure 1  $(30 + 6.25) \times 4$
 $36.25 \times 4 = \boxed{145}$

Figure 2 

SA $2\pi rh + 2\pi r^2$
 $2\pi(1.25)(3) + \pi(1.25)^2$

$23.56 + 4.9 = 28.46$
~~28.46~~

$\times 4$
 $\boxed{113.88}$

Figure 3 

Front/Back
 $\begin{array}{c} \square \\ 2 \end{array}^3$

$(2 \times 3) \times 2 = 12$

side $\begin{array}{c} \square \\ 2 \end{array}^3$ $(2 \times 3) = 6$

top $\frac{1}{2}(2 \times 3) = \frac{1}{2}(6) = 3$

$12 + 6 + 2 = 20 \times 4 = \boxed{80}$

$145 + 113.85 + 80 = 278.85$

$400 - 278.85 = \boxed{121.15}$

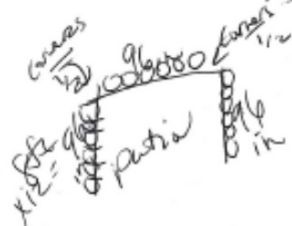
1 gallon

left over
Part B
units of volume

(22) $16 - 1.5 - 1 - 1.5 = 12 / 2 = 6$

$6 - 1 - 1 = 6$

$V = 6 \times 6 \times 8 = 288$



$96/16$ (each brick) $= 6$

$\times 3$

$18 + 1$

for 2 corners

19

$V = l \times w \times h$

$6 \times 6 \times 8 = 288$

$\times 19 \text{ Bricks}$

5472 in^3

$\underline{1728}$

So 1 bag 1 cubic ft

$12^3 \text{ in}^3 = 1728$

cubic inch

3.16 so **4 bags**

#23 order

13

5

3

1

6

2

4

it is an
angle
bisector

construction

#24 order 13

3

1

5

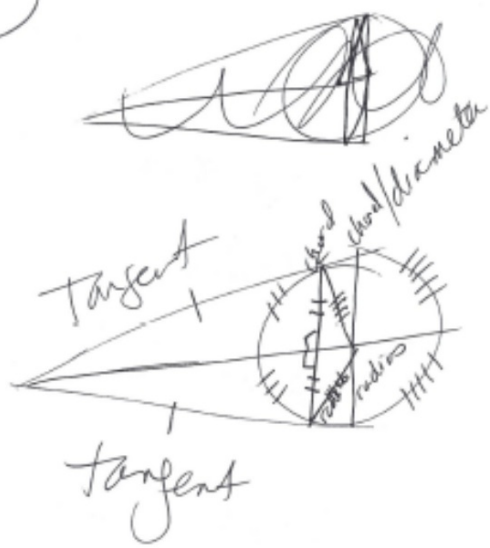
2

4

it is

an
perpendicular
bisector
construction

(25)



(27)



$$\begin{aligned} x(1.3) &= 1.3(x+1.3) \\ 1.3x &= 1.3x + 1.69 \\ -1.3x &-1.3x \end{aligned}$$

$$\frac{0.6x}{0.6} = \frac{1.69}{0.6}$$

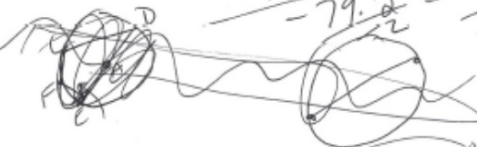
$$x = 2.82$$

(28)

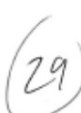


$$\begin{aligned} 140.4 &= \frac{1}{2}(360 - x - x) \\ 2(140.4) &= \frac{1}{2}(360 - 2x) \\ 280.8 &= \frac{360 - 2x}{2} \\ -360 &-360 \\ -79.2 &= \frac{-2x}{2} \end{aligned}$$

(29)



$$x = 39.6$$



Part B: $\angle D = \frac{1}{2} (50 + 34) = 42^\circ$
 $\angle F = 180 - 42 = 138^\circ$



$$2(30) - 20 = 40$$

$$\begin{array}{r} \angle D + \angle A = 90 \\ x + 40 = 90 \\ \underline{-40} \quad \underline{-40} \\ x = 50 \end{array}$$

(31)



$$\frac{360}{16} = 22.5$$

$$\frac{22.5}{360} \times \pi r^2$$

$$\frac{22.5}{360} \times \pi (11.5)^2 =$$

$$8.27\pi \text{ or } 25.97$$

(32) $x^2 + 2x + 1 + y^2 - 4y + 4 = 4$
 $\left(\frac{x}{2}\right)^2 = 1 \quad (x+1)(x+1) + (y-2)(y-2) \quad \left(\frac{y}{2}\right)^2 = 4$
 $(x+1)^2 + (y-2)^2 = -E + 4 + 1$
 $0 = -E + 5$
 $E = 5$
 $E < 5$

(33) ~~$x^2 + y^2 = 1$~~

Equation of a circle

$$(x-h)^2 + (y-k)^2 = r^2$$

$$(x-1)^2 + (y-2)^2 = 1^2$$

$$(x+1)^2 + (y-2)^2 = 1$$

(h, k)
Center
 $r = \text{radius}$

$$(34) (x-h)^2 + (y-k)^2 = r^2$$

$$(x-2)^2 + (y-5)^2 = r^2$$

use distance formula to
find radius

$$(-2, -5) \quad (5, 0)$$

$$x_1, y_1$$

$$x_2, y_2$$

$$(\sqrt{74})^2$$

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$(5 - -2)^2 + (0 - -5)^2$$

$$(7)^2 + (5)^2$$

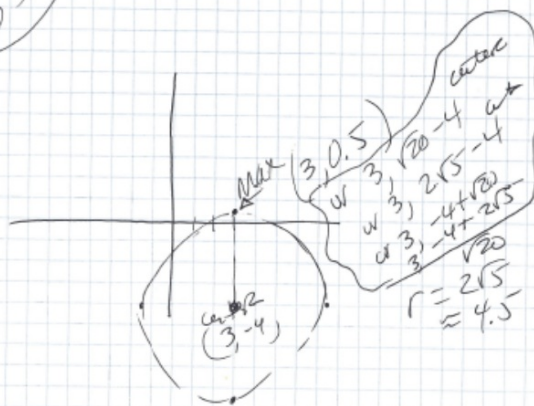
$$49 + 25 = r^2$$

$$74 \quad r = \sqrt{74}$$

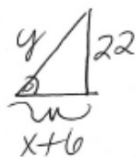
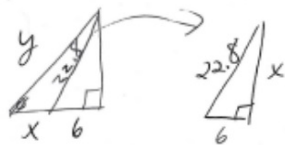
$$(x+2)^2 + (y+5)^2 = 74$$

(35) $x^2 - 6x + y^2 + 8y$
 $(-\frac{6}{2})^2 = 9$ $x^2 - 6x + 9$ $(\frac{8}{2})^2 = 16$ $y^2 + 8y + 16$
 $(x-3)(x-3)$ $(y+4)(y+4)$
 $(x-3)^2 + (y+4)^2 = -5 + 9 + 16$
 $(x-3)^2 + (y+4)^2 = (\sqrt{20})^2$
 $(x-3)^2 + (y+4)^2 = (2\sqrt{5})^2$
 $(x-h)^2 + (y-k)^2 = r^2$
 Center $(3, -4)$ radius $= 2\sqrt{5}$ *graph*

(35)



(36)



$$a^2 + b^2 = c^2$$

$$x^2 + 6^2 = (22.8)^2$$

$$x^2 + 36 = 519.84$$

$$\quad -36 \quad -36$$

$$x^2 = 483.84$$

$$x = 22$$

$$(A) \sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{22}{x+y}$$

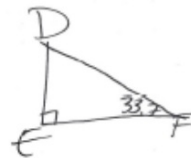
$$(F) \tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{22}{x+6}$$

(37)



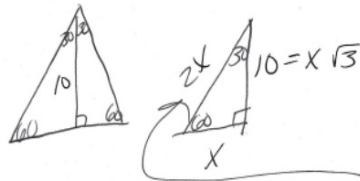
$$\sin 33.7^\circ = \frac{\text{opp}}{\text{hyp}} = \frac{BC}{AB}$$

$$\frac{BC}{AC} = \frac{DE}{EF}$$



$$\sin 33.7^\circ = \frac{\text{opp}}{\text{hyp}} = \frac{DE}{DF}$$

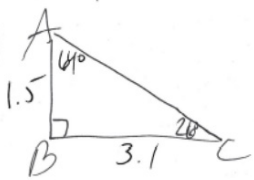
38



$$\frac{X\sqrt{3}}{\sqrt{3}} = \frac{10}{\sqrt{3}} \quad \frac{\sqrt{3}}{\sqrt{3}} = \frac{10\sqrt{3}}{\sqrt{9}} \quad \cancel{X} = \frac{10\sqrt{3}}{3}$$

$$2\left(\frac{10\sqrt{3}}{3}\right) = \boxed{\frac{20\sqrt{3}}{3}}$$

39



Part A: $\angle C = \frac{\text{opp}}{\text{adj}}$

$$\tan^{-1} \angle C = \frac{1.5}{3.1} = 26^\circ$$

$$\tan^{-1} \angle A = \frac{3.1}{1.5} = 64^\circ$$

$$x \cdot \sin 26 = \frac{\text{opp}}{\text{hyp}} \frac{1.5}{x} \cdot x$$

$$\frac{x(\sin 26)}{(\sin 26)} = \frac{1.5}{(\sin 26)} = 3.44 \quad (1.5)^2 + (3.1)^2 = c^2$$

$$2.25 + 9.61 = c^2$$

$$\frac{11.86}{11.86} = \frac{c^2}{(3.44)^2}$$

(41) A) False

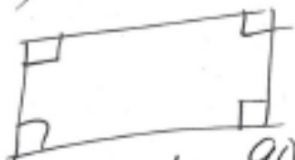


a trapezoid
is a
quadrilateral

Counter-
example →

that doesn't
have 4 right angles

D) False



all $\angle$'s 90°

not $\cong$

all $\angle$'s $= 90^\circ$

Counter-example ↗