

## Special Right Triangles P2

Tuesday, April 04, 2023 7:48 PM

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Special  
Right



# Special Right Triangles

## Workbook pages 135-137



## MA.912.T.1.2

Solve mathematical and real-world problems involving right triangles using trigonometric ratios and the Pythagorean Theorem.

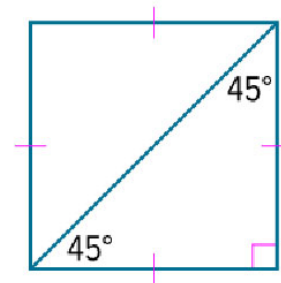
### Content Objective

Students will solve problems by using the properties of  $45^\circ - 45^\circ - 90^\circ$  and  $30^\circ - 60^\circ - 90^\circ$  triangles.

## Learn

### $45^\circ - 45^\circ - 90^\circ$ Triangles

The diagonal of a square forms two congruent isosceles right triangles. Because the base angles of an isosceles triangle are congruent, the measure of each acute angle is  $90^\circ \div 2$  or  $45^\circ$ . Such a special right triangle is known as a  **$45^\circ - 45^\circ - 90^\circ$  triangle**.

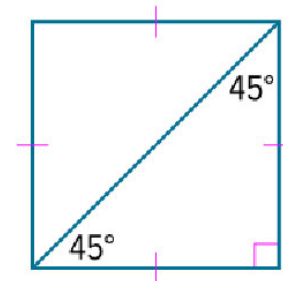


## Learn

### $45^\circ - 45^\circ - 90^\circ$ Triangles

#### Theorem 9.5: $45^\circ - 45^\circ - 90^\circ$ Triangle Theorem

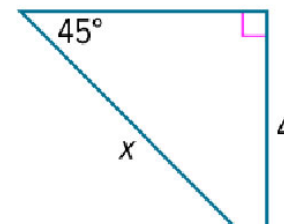
In a  $45^\circ - 45^\circ - 90^\circ$  triangle, the legs  $\ell$  are congruent and the length of the hypotenuse  $h$  is  $\sqrt{2}$  times the length of a leg.



## Example 1

Find the Hypotenuse Length Given an Angle Measure

Find the value of  $x$ .

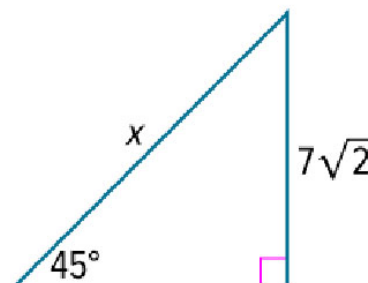


### Example 1

Find the Hypotenuse Length Given an Angle Measure

#### Check

Find the value of  $x$ .

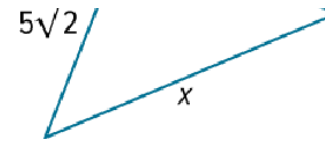


### Example 2

Find the Hypotenuse Length Given a Side Measure

Find the value of  $x$ .



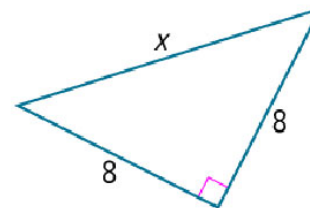


## Example 2

Find the Hypotenuse Length Given a Side Measure

### Check

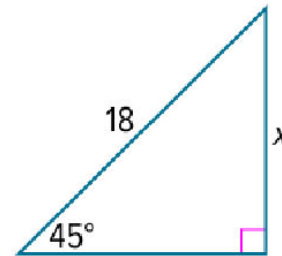
Find the value of  $x$ .



## Example 3

Find Leg Lengths in a  $45^\circ - 45^\circ - 90^\circ$  Triangle

Find the value of  $x$ .

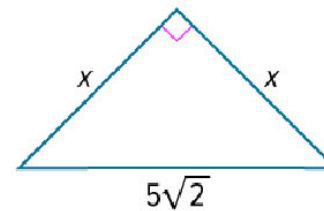


### Example 3

Find Leg Lengths in a  $45^\circ - 45^\circ - 90^\circ$  Triangle

### Check

Find the value of  $x$ .



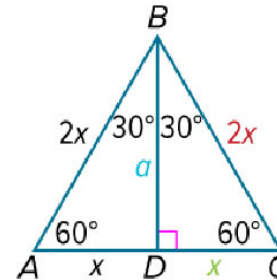
## Learn

### $30^\circ - 60^\circ - 90^\circ$ Triangles

A  **$30^\circ - 60^\circ - 90^\circ$  triangle** is a special right triangle or right triangle with side lengths that share a special relationship. You can use an equilateral triangle to find this relationship.

When an altitude is drawn from any vertex of an equilateral triangle, two congruent  $30^\circ - 60^\circ - 90^\circ$  triangles are formed. In the figure,

$\triangle ABD \cong \triangle CBD$ , so  $\overline{AD} \cong \overline{CD}$ . If  $AD = x$ , then  $CD = x$  and  $AC = 2x$ . Because  $\triangle ABC$  is equilateral,  $AB = 2x$  and  $BC = 2x$ .



*(continued on the next slide)*

## Learn

### $30^\circ - 60^\circ - 90^\circ$ Triangles

Use the Pythagorean Theorem to find  $a$ , the length of the altitude  $\overline{BD}$ , which is also the longer leg of  $\triangle BDC$ .

$$a^2 + x^2 = (2x)^2$$

$$a^2 + x^2 = 4x^2$$

$$a^2 = 3x^2$$

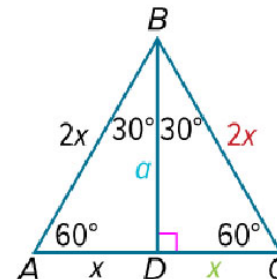
$$a = x\sqrt{3}$$

Pythagorean Theorem

Simplify.

Subtract  $x^2$  from each side.

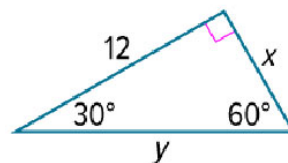
Simplify.



**Example 4**

Find Leg Lengths in a  $30^\circ - 60^\circ - 90^\circ$  Triangle

Find the values of  $x$  and  $y$ .

**Example 4**

Find Leg Lengths in a  $30^\circ - 60^\circ - 90^\circ$  Triangle

**Check**

Find the values of  $x$  and  $y$ .

