Monday, January 16, 2023 11:45 AM





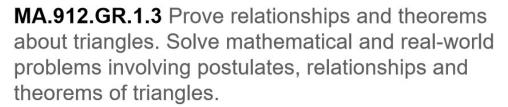
Lesson 5.2 Congruent Triangles Pages 281-286



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Florida's B.E.S.T. Standards for Mathematics



MA.912.GR.1.6 Solve mathematical and real-world problems involving congruence or similarity in two-dimensional figures.

MA.912.GR.2.6 Apply rigid transformations to map one figure onto another to justify that the two figures are congruent.

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Lesson Objectives

Content Objective

Students will use congruence criteria and the Third Angles Theorem to solve problems.

Language Objectives

 Students explain congruence between triangles based on their corresponding parts using same, equal, corresponding, and congruent.

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Learn

Interior Angles of Triangles

Key Concept: Congruent Triangles

Two triangles are congruent if and only if their corresponding parts are congruent.

For triangles, we say Corresponding parts of congruent triangles are congruent, or CPCTC.

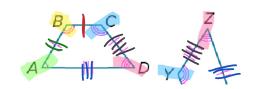
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Example 1

Identify Corresponding Congruent Parts

Show that the polygons are congruent by identifying all the congruent corresponding parts. Then write a







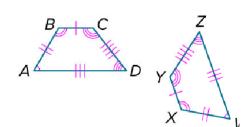
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Example 1

Identify Corresponding Congruent Parts

Angles:
$$\angle A \cong \angle W$$
; Sides: $\overline{BC} \cong \overline{XY}$; $\angle B \cong \angle X$; $\overline{AB} \cong \overline{WX}$; $\angle C \cong \angle Y$; $\overline{DA} \cong \overline{ZW}$; $\angle D \cong \angle Z$ $\overline{CD} \cong \overline{YZ}$



All corresponding parts of the two polygons are congruent. Therefore, polygon $ABCD \cong \text{polygon } WXYZ$.

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Example 2

Use Corresponding Parts of Congruent

Triangles



Find the values of x and y.

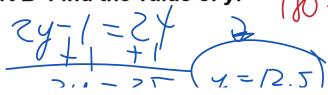
78+90=16



Part B Find the value of y.

180-168-(12)







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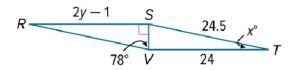
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Example 2

Use Corresponding Parts of Congruent Triangles

Part A Find the value of x.



$$\angle T \cong \angle R$$

$$m \angle T = m \angle R$$

$$= 180^{\circ} - 90^{\circ} - 78^{\circ}$$

 $= 12^{\circ}$

CPCTC

Definition of congruence

Triangle Angle-Sum

Theorem

Solve.

The value of x is 12.

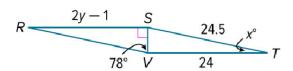
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Example 2

Use Corresponding Parts of Congruent Triangles

Part B Find the value of y.



$$\overline{RS} \cong \overline{TV}$$
 $RS = TV$
 $2y - 1 = 24$
 $v = 12.5$

CPCTC

Definition of congruence

Substitution

Solve.

The value of y is 12.5.

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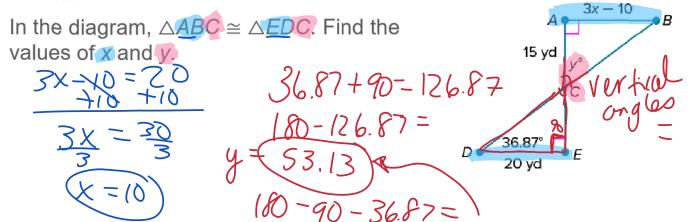


Use Corresponding Parts of Congruent



rnangies

Check



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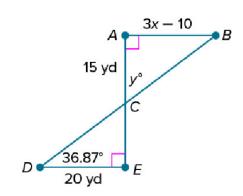
Example 2

Use Corresponding Parts of Congruent Triangles

Check

In the diagram, $\triangle ABC \cong \triangle EDC$. Find the values of x and y.

$$x = 10$$
; $y = 53.13$



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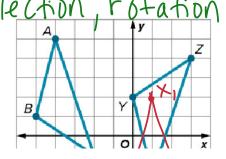
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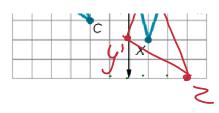
Example 3

Justify Congruence Using Rigid Transformations

Is $\triangle ABC \cong \triangle XYZ$? Justify your answer using rigid transformations.

(2) Translation Rule (X-5 4+3)





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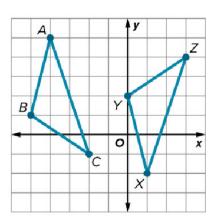
Justify Congruence Using Rigid Transformations

Identify the rigid transformations that could map $\triangle XYZ$ onto $\triangle ABC$.

If X and A are corresponding vertices, we need to reorient $\triangle XYZ$ so that X is the topmost vertex of the triangle. Reflect $\triangle XYZ$ in the x-axis.

$$X(1, -2) \rightarrow X'(1, 2)$$

 $Y(0, 2) \rightarrow Y'(0, -2)$
 $Z(3, 4) \rightarrow Z'(3, -4)$



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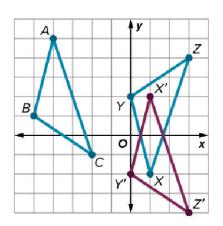
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Example 3

Justify Congruence Using Rigid

Transformations X - S, Y + ZEach vertex of $\triangle X'Y'Z'$ can be mapped 5, onto $\triangle ABC$ with a translation along the

We know that rigid transformations preserve side lengths and angle measures. Therefore, after the reflection and translation the corresponding sides and corresponding angles of $\triangle ABC$ and the image of $\triangle XYZ$ coincide. Therefore, $\triangle ABC \cong \triangle XYZ$.



Learn

Third Angles Theorem and Triangle Congruence

Theorem 5.3: Third Angles Theorem

Words	If two angles of one triangle are congruent to two angles of a second triangle, then the third angles of the triangles are congruent.
Example	If $\angle C \cong \angle K$ and $\angle B \cong \angle J$, then $\angle A \cong \angle L$.

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Learn

Third Angles Theorem and Triangle Congruence



Reflexive Property of Triangle Congruence

 $\triangle ABC \cong \triangle ABC$

Symmetric Property of Triangle Congruence

If $\triangle ABC \cong \triangle EFG$, then $\triangle EFG \cong \triangle ABC$.

Transitive Property of Triangle Congruence

If $\triangle ABC \cong \triangle EFG$ and $\triangle EFG \cong \triangle JKL$, then $\triangle ABC \cong \triangle JKL$.

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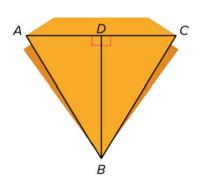
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Example 4

Use the Third Angles Theorem



a party she is hosting. If $\angle ABD \cong \angle CBD$ and $m\angle BAD = 58^{\circ}$, find $m\angle CBD$.



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Example 4

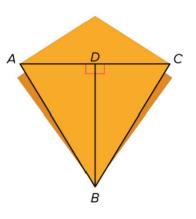
Use the Third Angles Theorem

$$m \angle BCD = 58^{\circ}$$

 $m \angle CBD + 58^{\circ} = 90^{\circ}$
 $m \angle CBD = 32^{\circ}$

The measure of $\angle CBD$ is 32°.

Substitute. Substitute. Solve.



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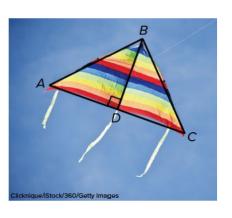
Example 4

Use the Third Angles Theorem

Check

KITES In the kite shown, $\angle BAD \cong \angle BCD$ and $m\angle BCD = 45^{\circ}$. Find $m\angle ABD$.





Example 4

Use the Third Angles Theorem

Check

KITES In the kite shown, $\angle BAD \cong \angle BCD$ and $m\angle BCD = 45^{\circ}$. Find $m\angle ABD$.

$$m \angle ABD = 45^{\circ}$$

