

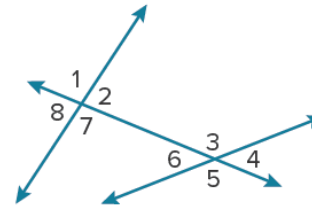
## Example 2

### Classify Angle Pair Relationships

#### Check

Classify the relationship between each pair of angles as *alternate interior*, *alternate exterior*, *corresponding*, or *consecutive interior angles*.

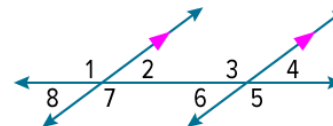
- a.  $\angle 1$  and  $\angle 5$      **alternate exterior angles**
- b.  $\angle 2$  and  $\angle 4$      **corresponding angles**



## Learn

### Angles and Parallel Lines

If two lines are parallel and cut by a transversal, then there are special relationships in the angle pairs formed by the lines.



#### Theorem 3.14: Corresponding Angles Theorem

If two parallel lines are cut by a transversal, then each pair of corresponding angles is congruent.

$$\begin{aligned}\angle 1 &\cong \angle 3, \\ \angle 2 &\cong \angle 4, \\ \angle 5 &\cong \angle 7, \\ \angle 6 &\cong \angle 8\end{aligned}$$

## Learn

### Angles and Parallel Lines

#### Theorem 3.15: Alternate Interior Angles Theorem

If two parallel lines are cut by a transversal, then each pair of alternate interior angles is congruent.

$$\begin{aligned}\angle 2 &\cong \angle 6, \\ \angle 3 &\cong \angle 7\end{aligned}$$

#### Theorem 3.16: Consecutive Interior Angles Theorem

If two parallel lines are cut by a transversal, then each pair of consecutive interior angles is supplementary.

$$\begin{aligned}\angle 2 \text{ and } \angle 3, \\ \angle 6 \text{ and } \angle 7\end{aligned}$$

## Learn

### Angles and Parallel Lines

#### Theorem 3.17: Alternate Exterior Angles Theorem

If two parallel lines are cut by a transversal, then each pair of alternate exterior angles is congruent.

$$\begin{aligned}\angle 1 &\cong \angle 5, \\ \angle 4 &\cong \angle 8\end{aligned}$$

## Learn

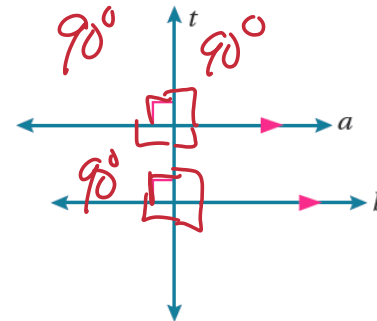
### Angles and Parallel Lines

A special relationship also exists when the transversal of two parallel lines is a perpendicular line.

#### Theorem 3.18: Perpendicular Transversal Theorem

In a plane, if a line is perpendicular to one of two parallel lines, then it is perpendicular to the other.

**Example** If  $a \parallel b$  and  $a \perp t$ , then  $b \perp t$ .

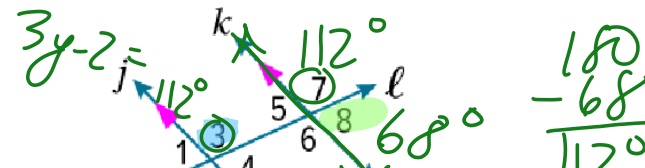


## Example 5

### Find Values of Variables

Use the figure to find the value of the indicated variable. Justify your reasoning.

a. If  $m\angle 3 = (4x + 7)^\circ$  and  $m\angle 6 = (5x - 13)^\circ$ .



find the value of  $x$ .

b. Find the value of  $y$  if  $m\angle 8 = 68^\circ$  and  $m\angle 3 = (3y - 2)^\circ$ .

Corresponding  
 $\angle 3 = \angle 7$

$$\begin{array}{r} 3y - 2 = 112 \\ +2 \quad +2 \\ \hline 3y = 114 \\ \hline y = 38 \end{array}$$

Alternate  
Interior  
 $4x + 7 = 5x - 13$   
 $+7 \quad -7$

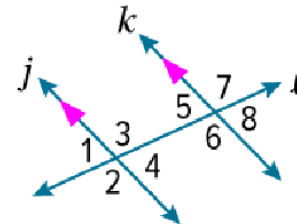
$$\begin{array}{r} 4x = 5x - 20 \\ -5x \quad -5x \\ \hline -1x = -20 \\ \hline x = 20 \end{array}$$

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### Example 5

Find Values of Variables

a. If  $m\angle 3 = (4x + 7)^\circ$  and  $m\angle 6 = (5x - 13)^\circ$ , find the value of  $x$ .



$$\angle 3 \cong \angle 6$$

$$m\angle 3 = m\angle 6$$

$$(4x + 7)^\circ = (5x - 13)^\circ$$

$$x = 20$$

Alternate Interior Angles Theorem

Definition of congruent angles

Substitution

Solve.

### Example 5

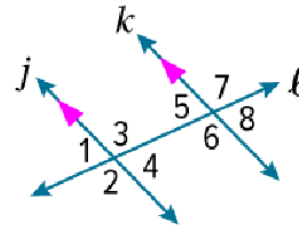
Find Values of Variables

b. Find the value of  $y$  if  $m\angle 8 = 68^\circ$  and  $m\angle 3 = (3y - 2)^\circ$ .

$$\angle 5 \cong \angle 8 \quad \text{Vertical Angles Theorem}$$

$$m\angle 5 = m\angle 8 \quad \text{Definition of congruent angles}$$

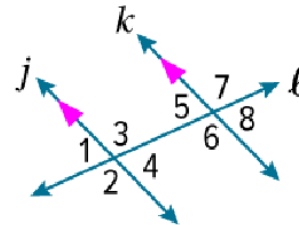
$$m\angle 5 = 68^\circ \quad \text{Substitution}$$



## Example 5

### Find Values of Variables

Because lines  $j$  and  $k$  are parallel,  $\angle 5$  and  $\angle 3$  are supplementary by the Consecutive Interior Angles Theorem.



$$\begin{aligned} m\angle 3 + m\angle 5 &= 180^\circ \\ (3y - 2)^\circ + 68^\circ &= 180^\circ \\ 3y^\circ + 66^\circ &= 180^\circ \\ y &= 38 \end{aligned}$$

Definition of supplementary angles

Substitution

Simplify.

Solve.