

## Lesson 3.7 Parallel Lines and Transversals

Sunday, November 27, 2022 4:47 PM

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ParallelLi...

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# Parallel Lines and Transversals



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## Learn

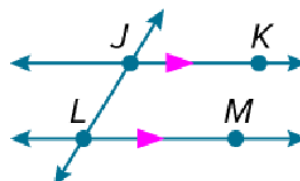
### Parallel Lines and Transversals

If two lines do not intersect, then they are either parallel or skew.

#### Parallel and Skew

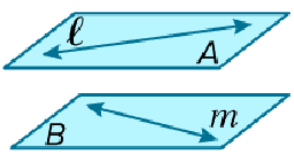
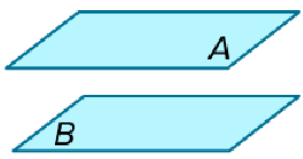
**Parallel lines** are coplanar lines that do not intersect.

**Example**  $\overleftrightarrow{JK} \parallel \overleftrightarrow{LM}$



## Learn

### Parallel Lines and Transversals

Parallel and Skew	
<p><b>Skew lines</b> are lines that do not intersect and are not coplanar.</p> <p><b>Example</b> Lines <math>\ell</math> and <math>m</math> are skew.</p>	
<p><b>Parallel planes</b> are planes that do not intersect.</p> <p><b>Example</b> Planes <math>\mathcal{A}</math> and <math>\mathcal{B}</math> are parallel.</p>	

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### Parallel Lines and Transversals

A line that intersects two or more lines in a plane at different points is called a **transversal**. In the diagram below, line  $t$  is a transversal of lines  $q$  and  $r$ . Line  $t$  forms a total of eight angles with lines  $q$  and  $r$ . These angles and specific pairings of these angles are given special names.

## Learn

### Parallel Lines and Transversals

inside  
↑  
Outside  
↖  
next to  
↖

## Transversal Angle Pair Relationships

Four **interior angles** lie in the region between lines  $q$  and  $r$ .

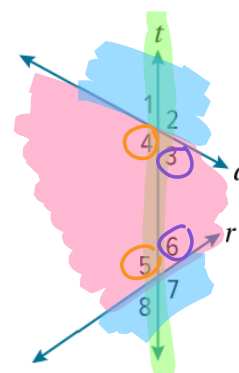
$\angle 3, \angle 4, \angle 5, \angle 6$

Four **exterior angles** lie in the two regions that are not between lines  $q$  and  $r$ .

$\angle 1, \angle 2, \angle 7, \angle 8$

**Consecutive interior angles** are interior angles that lie on the same side of transversal  $t$ .

$\angle 4$  and  $\angle 5,$   
 $\angle 3$  and  $\angle 6$



## Learn

### Parallel Lines and Transversals

inside  
opp.  
↖  
outside  
opp.  
↖

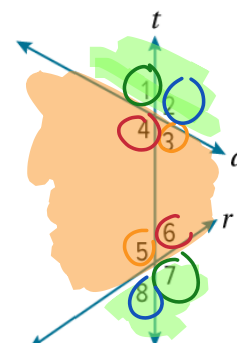
## Transversal Angle Pair Relationships

**Alternate interior angles** are nonadjacent interior angles that lie on opposite sides of transversal  $t$ .

$\angle 3$  and  $\angle 5,$   
 $\angle 4$  and  $\angle 6$

**Alternate exterior angles** are nonadjacent exterior angles that lie on opposite sides of transversal  $t$ .

$\angle 1$  and  $\angle 7,$   
 $\angle 2$  and  $\angle 8$



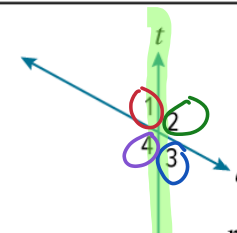
## Learn

### Parallel Lines and Transversals

## Transversal Angle Pair Relationships

**Corresponding angles** lie on the same side of transversal  $t$  and on the same side of lines  $q$  and  $r$ .

$\angle 1$  and  $\angle 5,$   
 $\angle 2$  and  $\angle 6,$   
 $\angle 3$  and  $\angle 7,$   
 $\angle 4$  and  $\angle 8$



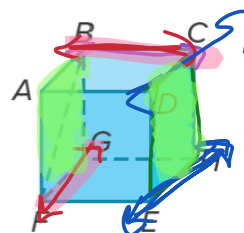


## Example 1

Identify Parallel and Skew Relationships

Identify each of the following using the cube shown. Assume lines and planes that appear to be parallel or perpendicular are parallel or perpendicular, respectively.

- a. all lines skew to  $\overleftrightarrow{BC}$  *one*  $\overleftrightarrow{FG}$
- b. all lines parallel to  $\overleftrightarrow{EH}$  *one*  $\overleftrightarrow{CD}$
- c. all planes parallel to plane  $DCH$  *one*   
 Plane  $ABG$



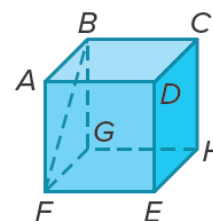
## Example 1

Identify Parallel and Skew Relationships

- a. all lines skew to  $\overleftrightarrow{BC}$    
  $\overleftrightarrow{AF}$ ,  $\overleftrightarrow{DE}$ ,  $\overleftrightarrow{FG}$ , and  $\overleftrightarrow{HE}$
- b. all lines parallel to  $\overleftrightarrow{EH}$    
  $\overleftrightarrow{AB}$ ,  $\overleftrightarrow{CD}$ , or  $\overleftrightarrow{FG}$

- c. all planes parallel to plane  $DCH$

Plane  $ABG$  is the only plane parallel to plane  $DCH$ .

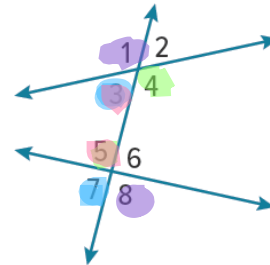


## Example 2

### Classify Angle Pair Relationships

A.I. Classify the relationship between each pair of angles as alternate interior, alternate exterior, A.E., corresponding, or consecutive interior angles. C.I.A.

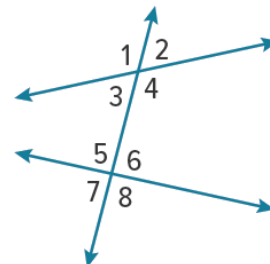
$\angle 4$  and  $\angle 5$  ALT. Interior  $\angle$ 's  
 $\angle 3$  and  $\angle 7$  Corresponding  
 $\angle 3$  and  $\angle 5$  Consecutive  
 $\angle 1$  and  $\angle 8$  ALT. Exterior



## Example 2

### Classify Angle Pair Relationships

$\angle 4$  and  $\angle 5$  are alternate interior angles.  
 $\angle 3$  and  $\angle 7$  are corresponding angles.  
 $\angle 3$  and  $\angle 5$  are consecutive interior angles.  
 $\angle 1$  and  $\angle 8$  are alternate exterior angles.



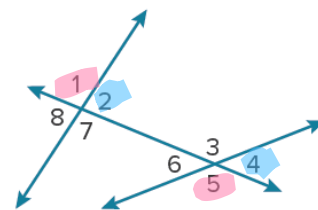
## Example 2

### Classify Angle Pair Relationships

### Check

Classify the relationship between each pair of angles as *alternate interior*, *alternate exterior*, *corresponding*, or *consecutive interior angles*.

- a.  $\angle 1$  and  $\angle 5$  *ALT. EXTERIOR*  
 b.  $\angle 2$  and  $\angle 4$  *corresponding.*



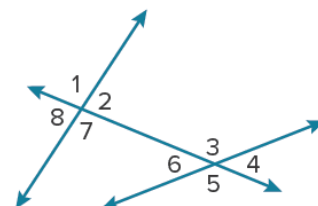
## Example 2

Classify Angle Pair Relationships

### Check

Classify the relationship between each pair of angles as *alternate interior*, *alternate exterior*, *corresponding*, or *consecutive interior angles*.

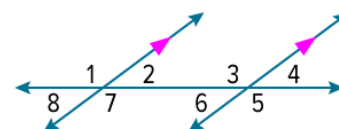
- a.  $\angle 1$  and  $\angle 5$  *alternate exterior angles*  
 b.  $\angle 2$  and  $\angle 4$  *corresponding angles*



## Learn

Angles and Parallel Lines

If two lines are parallel and cut by a transversal, then there are special relationships in the angle pairs formed by the lines.



### Theorem 3.14: Corresponding Angles Theorem

If two parallel lines are cut by a transversal, then each pair of corresponding angles is congruent.

$$\begin{aligned}\angle 1 &\cong \angle 3, \\ \angle 2 &\cong \angle 4,\end{aligned}$$