

$$\sqrt{90} \quad x \cdot x$$

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Do not remove this bar**Explore 1 Investigating an Isosceles Right Triangle**

Discover relationships that always apply in an isosceles right triangle.

- (A) The figure shows an isosceles right triangle. Identify the base angles, and use the fact that they are complementary to write an equation relating their measures.

$$1x + 1x = 90 \quad \frac{2x}{2} = \frac{90}{2}$$

- (B) Use the Isosceles Triangle Theorem to write a different equation relating the base angle measures.

$$90 + x + x = 180$$

- (C) What must the measures of the base angles be? Why?

$$\frac{90}{2} = \frac{90}{2}$$

- (D) Use the Pythagorean Theorem to find the length of the hypotenuse in terms of the length of each leg, x .

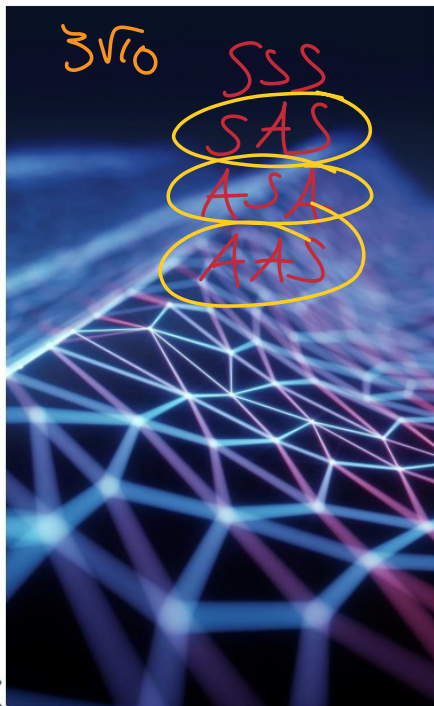
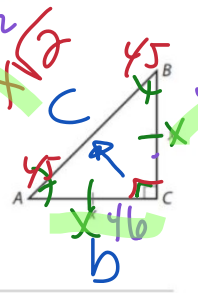
$$a^2 + b^2 = c^2$$

$$x^2 + x^2 = c^2$$

$$2x^2 = c^2$$

$$\sqrt{2x^2} = c$$

$$c = x\sqrt{2}$$



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Do not remove this bar**Explore 2 Investigating Another Special Right Triangle**

Discover relationships that always apply in a right triangle formed as half of an equilateral triangle.

- (A) $\triangle ABD$ is an equilateral triangle and \overline{BC} is a perpendicular from B to \overline{AD} . Determine all three angle measures in $\triangle ABC$.

$$C = 90 \quad \angle B = 30$$

- (B) Explain why $\triangle ABC \cong \triangle DBC$.

$$SAS = AB = BD$$

$$BC = BC \quad \text{Reflexive Prop}$$

- (C) Let the length of \overline{AC} be x . What is the length of \overline{AB} , and why?

$$AD \text{ is } 2x \text{ because } AC = DC$$

- (D) Using the Pythagorean Theorem, find the length of \overline{BC} .

$$a^2 + x^2 = (2x)^2$$

$$a^2 + x^2 = 4x^2$$

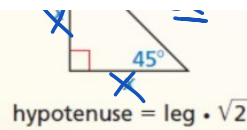
**Theorem****Theorem 9.4 45°-45°-90° Triangle Theorem**In a 45°-45°-90° triangle, the hypotenuse is $\sqrt{2}$ times as long as each leg.

$$a^2 = 3x^2$$

$$a = \sqrt{3x^2}$$

$$a = x\sqrt{3}$$

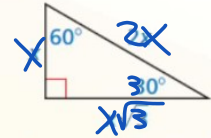
Proof Ex. 19, p. 476



Theorem

Theorem 9.5 30°-60°-90° Triangle Theorem

In a 30°-60°-90° triangle, the hypotenuse is twice as long as the shorter leg, and the longer leg is $\sqrt{3}$ times as long as the shorter leg.

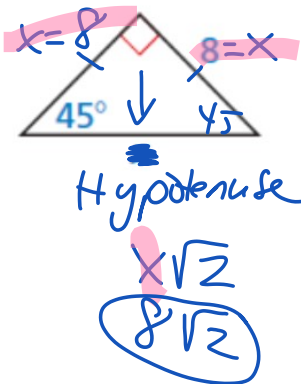


hypotenuse = shorter leg $\cdot 2$
longer leg = shorter leg $\cdot \sqrt{3}$

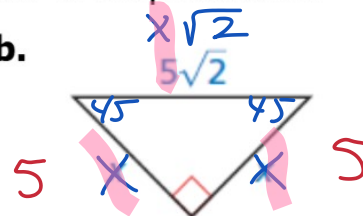
Proof Ex. 21, p. 476

Find the value of x . Write your answer in simplest form.

a.



b.



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Find the values of x and y . Write your answer in simplest form.

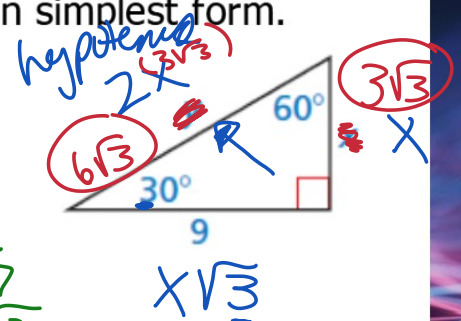
$$\frac{x\sqrt{3}}{\sqrt{3}} = \frac{9}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \frac{9\sqrt{3}}{3} = 3\sqrt{3}$$

$$(x\sqrt{3})^2 = (9)^2$$

$$\frac{x^2 \cdot 3}{3} = 81$$

$$x^2 = 27$$

$$x = \sqrt{27} = 3\sqrt{3}$$

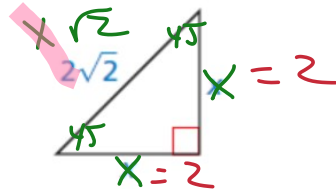


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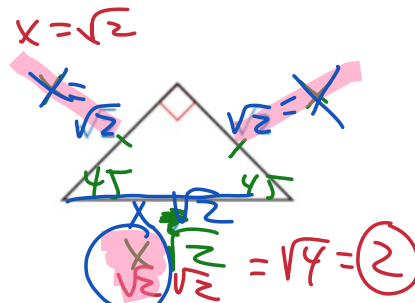
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Find the value of the variable. Write your answer in simplest form.

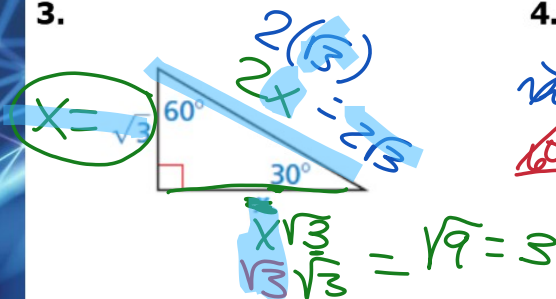
1.



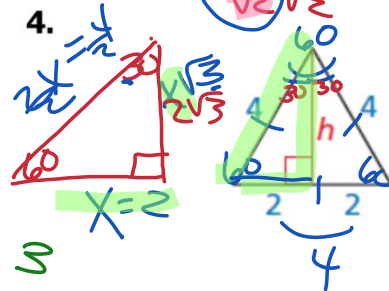
2.



3.



4.



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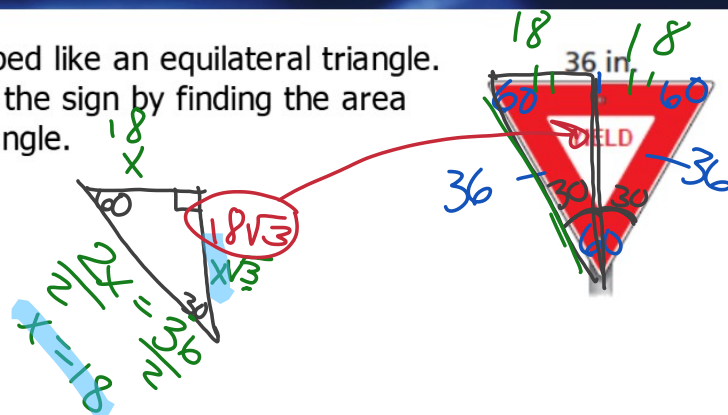
The road sign is shaped like an equilateral triangle. Estimate the area of the sign by finding the area of the equilateral triangle.

$$A = \frac{1}{2}bh$$

$$A = \frac{1}{2}(36)(18\sqrt{3})$$

$$A = (18)(18\sqrt{3})$$

$$A = 324\sqrt{3}$$



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