

Date: 10/22/20

### Lesson 3.4 Perpendicular Lines

**Learning Intent (Target):** Today I will be able to discover properties of perpendicular lines.

**Success Criteria:** I'll know I'll have it when I'll be able to use theorems about perpendicular lines to determine the distance between a point and a line on the coordinate plane.

**Accountable Team Task:** Therefore, I can practice from interactive flip charts and geogebra investigations.

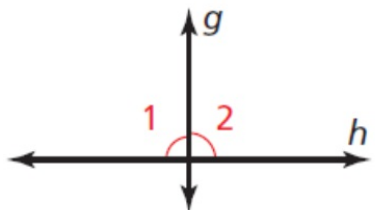
## Theorems

### Theorem 3.10 Linear Pair Perpendicular Theorem

If two lines intersect to form a linear pair of congruent angles, then the lines are perpendicular.

If  $\angle 1 \cong \angle 2$ , then  $g \perp h$ .

*Proof* Ex. 13, p. 153

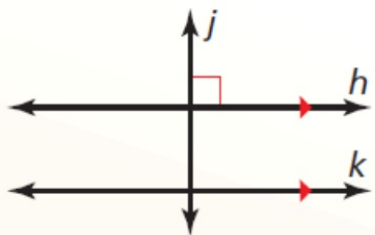


### Theorem 3.11 Perpendicular Transversal Theorem

In a plane, if a transversal is perpendicular to one of two parallel lines, then it is perpendicular to the other line.

If  $h \parallel k$  and  $j \perp h$ , then  $j \perp k$ .

*Proof* Example 2, p. 150; Question 2, p. 150

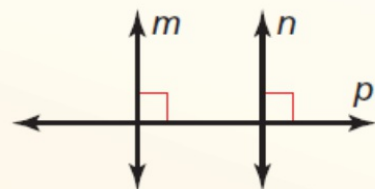


### Theorem 3.12 Lines Perpendicular to a Transversal Theorem

In a plane, if two lines are perpendicular to the same line, then they are parallel to each other.

If  $m \perp p$  and  $n \perp p$ , then  $m \parallel n$ .

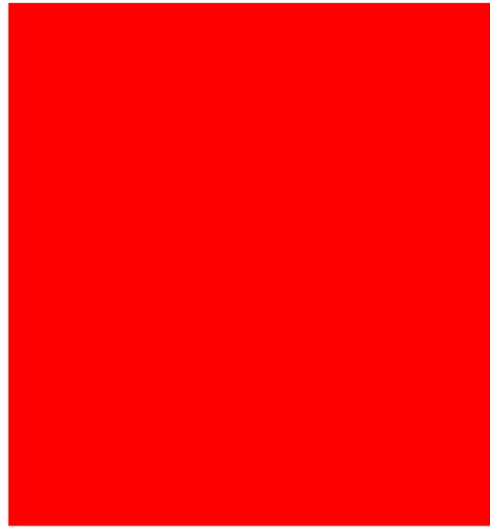
*Proof* Ex. 14, p. 153; Ex. 47, p. 162



Find the distance from point  $A$  to  $\overleftrightarrow{BD}$ .

**Line BD contains the coordinates -1,-3 and 2,0.**

**Point A is located at -3,3**



**First find the slope of BD which is 1.**

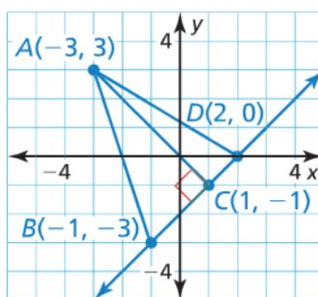
**The shortest distance is a perpendicular line from -3, 3 to the line segment BD**

**The negative reciprocal is -1 so use that slope to draw the line from -3, 3 to line segment BD.**

**The line now intersects BD at 1,-1.**

**Next step is using the distance formula to solve (or pythagorean theorem)**

Find the distance from point  $A$  to  $\overleftrightarrow{BD}$ .



### SOLUTION

Because  $\overline{AC} \perp \overleftrightarrow{BD}$ , the distance from point  $A$  to  $\overleftrightarrow{BD}$  is  $AC$ . Use the Distance Formula.

$$AC = \sqrt{(-3 - 1)^2 + [3 - (-1)]^2} = \sqrt{(-4)^2 + 4^2} = \sqrt{32} \approx 5.7$$

► So, the distance from point  $A$  to  $\overleftrightarrow{BD}$  is about 5.7 units.

**1.** Find the distance from point  $E$  to  $\overleftrightarrow{FH}$ .

**Line FH contains the coordinates  
0,3 and 2,1.**

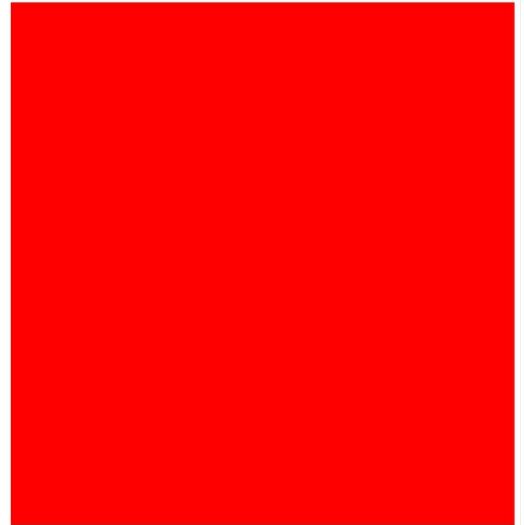
**Point E is located at -4,-3**

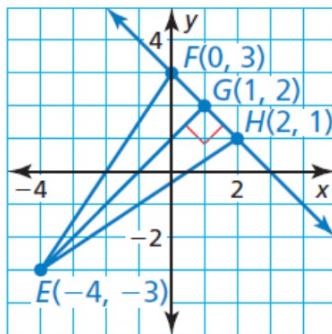
**Find the slope of FH first.**

**That is -1.**

**Next draw a perpendicular line from -4, -3  
using the negative reciprocal which is 1.**

**The line now intersects at line FH at 1,2.**





Use the distance formula or pythagorean theorem to solve for the distance. You should get about 7.1